

Equivalent Loading Frequencies to Simulate Asphalt Layer Pavement Responses Under Dynamic Traffic Loading

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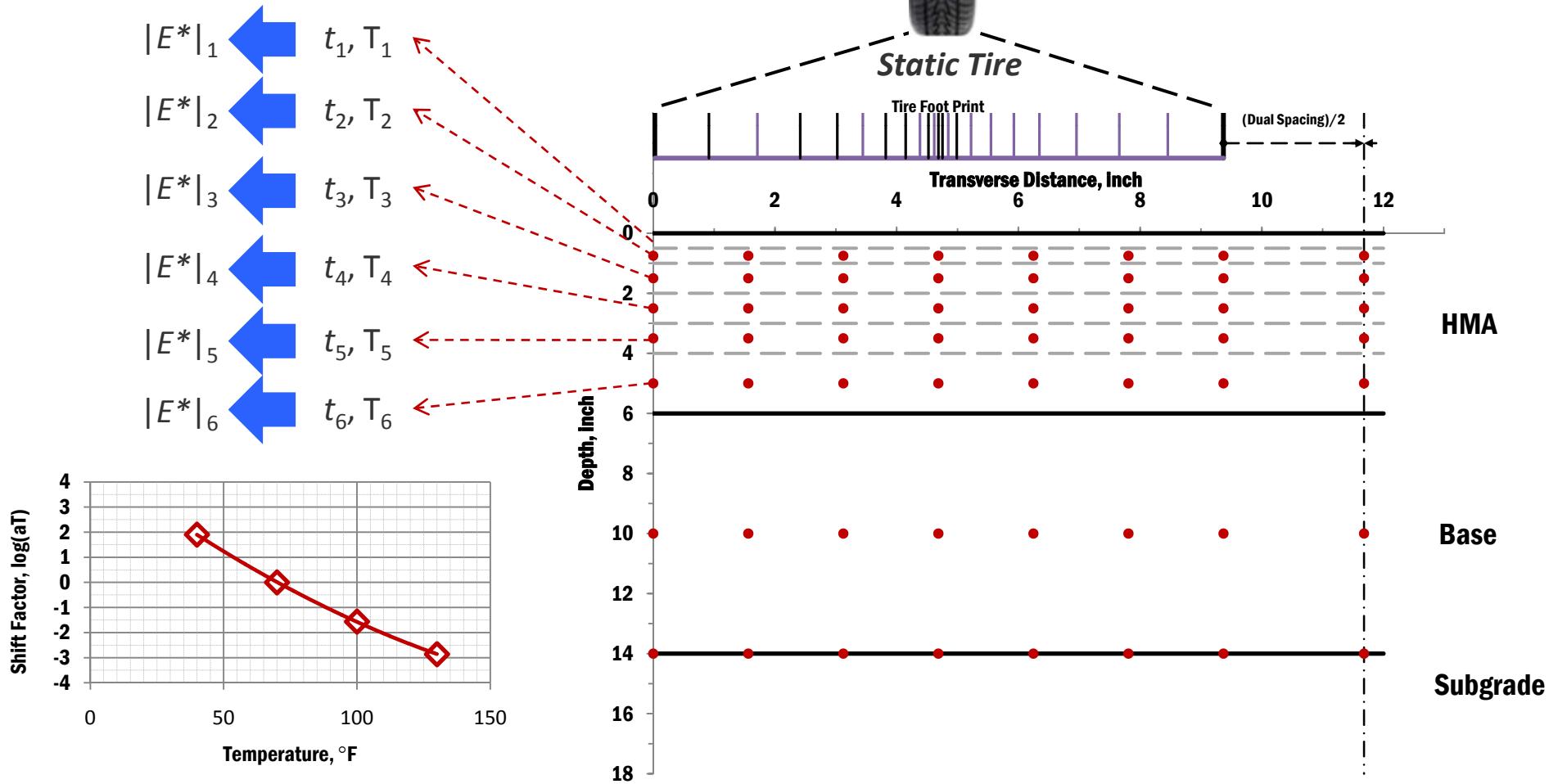
Introduction

- ***Dynamic response*** of AC pavements under moving load is a key component for accurate prediction of ***flexible pavement performance***.
- ***Reliable determination*** of pavement responses to moving load is essential for a successful mechanistic design procedure.
- ***Time and temperature dependency*** of asphalt must be considered in the mechanistic analysis response model.

AASHTO MEPDG Approach



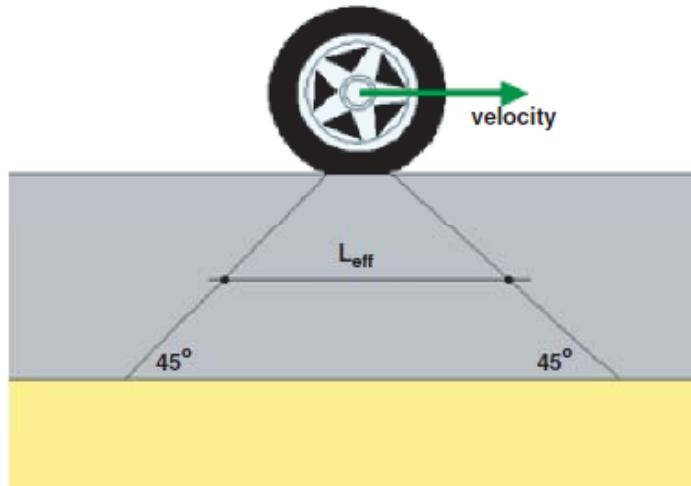
- Linear elastic analysis



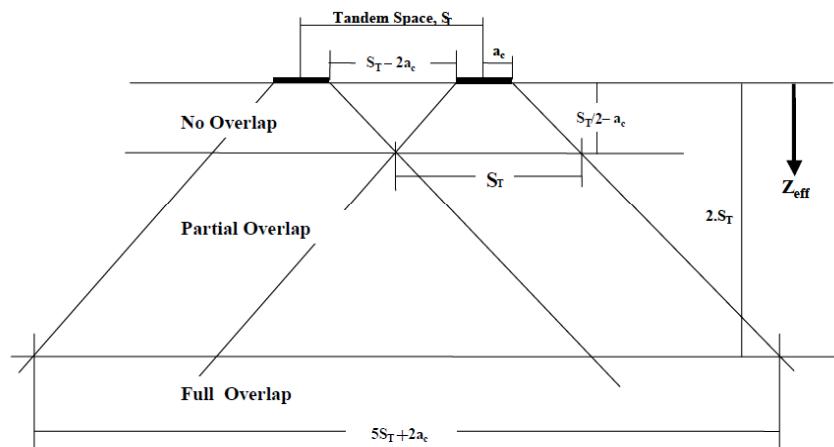
AASHTO MEPDG



- Vertical stress distribution used to estimate traffic-induced loading time.
 - Axle load configuration, Vehicle speed & Pavement structure



$$t = \frac{L_{eff}}{17.6 V_s} \quad \rightarrow \quad f = \frac{1}{t}$$



$$Z_{eff} = \sum_{i=1}^{n-1} \left(h_i \sqrt[3]{\frac{E_i}{E_{SG}}} \right) + h_n \sqrt[3]{\frac{E_n}{E_{SG}}}$$



Viscoelastic vs. Pseudo Analysis

Viscoelastic



HMA $|E^*| = f(\text{freq}) \text{ & } \zeta = f(\text{freq})$

CAB

SG

Pseudo-dynamic



HMA $|E^*|_{fp} = ?, \zeta_{fp} = ?$

CAB

SG

Pseudo-static



HMA $|E^*|_{fp} = ? \text{ } \zeta_{fp} = 0$

CAB

SG

Pavement responses ← ? → *Pavement responses* ← ? → *Pavement responses*



Objective

- Investigate the existence of one or more *predominant frequencies* (f_p) associated with the AC layer that controls the dynamic response of pavements.
- ***AC Critical Responses:***
 - Longitudinal & transverse tensile strains
 - Vertical compressive strains

Pavement Analysis

3D-Move Analysis Software



Complex surface

Asphalt Research Consortium

Home Outreach Project Team Software Publications Workshops Newsletters Contacts Links

Software

3D-Move

Free Softwares

3D-Move (NEW: Version 1.2) Now Available Online!

*Announcement to 3D-Move Users (Posted on August 29, 2010):
Inconsistency Between Text and Excel Output Files of Ver. 1.1*



Announcements

DISCUSSION GROUP at
3d-move.finndiscussion.com to
provide your feedback or
post your questions on the
3D-Move Analysis Software.

The last beta-version of the 3D-Move Analysis (ver 1.1) was released on July, 2010. In 3D-Move, output is provided in formats: Text and Excel. An inconsistency has inadvertently occurred when these two formats were integrated. The **inconsistency was present only in the Excel file**, while the **Text file output is correct**. The origin of the slip-up was traced to the allocation of the columns when the data sharing between Text and Excel output files occurred. Further, there were concerns about the units of the 3D-Move responses being not prominently displayed. These issues have been corrected and a modified beta-version of 3D-Move (ver 1.2) is now available for [download](#).

Pavement Analysis

3D-Move Analysis Software - Validation



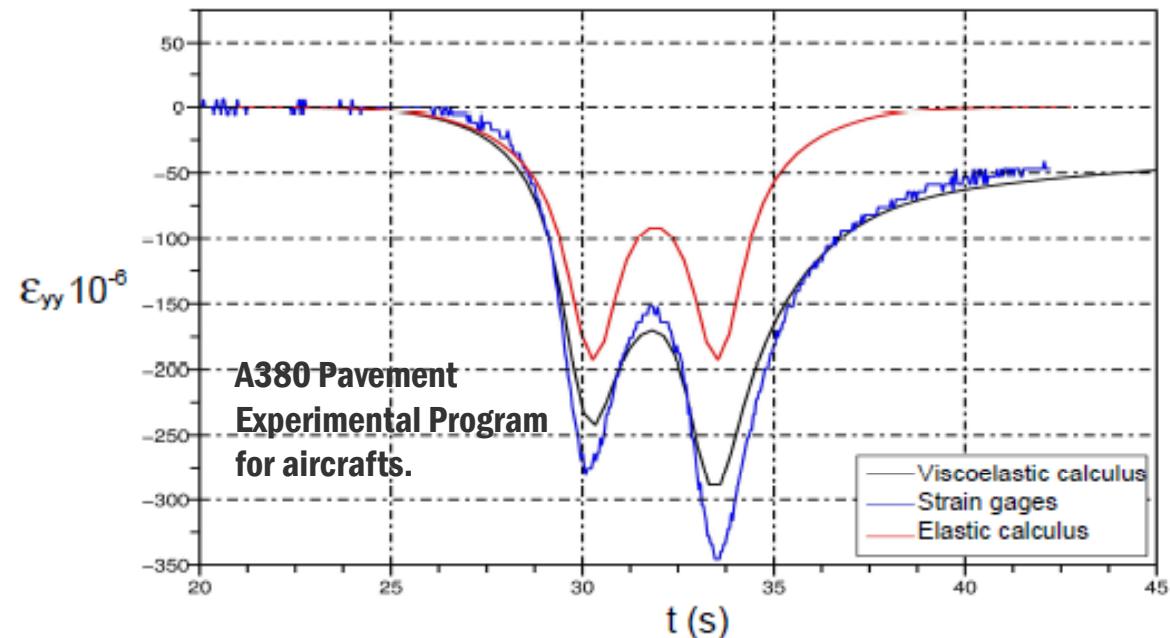
1. 3D-Move vs. ViscoRoute (2010)

- ViscoRoute: moving circular loaded areas with uniform contact pressure, viscoelastic material properties

Reference:

Chabot, A., Chupin, O., Deloffre, L., and Duhamel, D., "Viscoroute 2.0: a tool for the simulation of moving load effects on asphalt pavement," *Road Materials and Pavement Design an International Journal*, Volume 11/2, 2010, pp. 227-250.

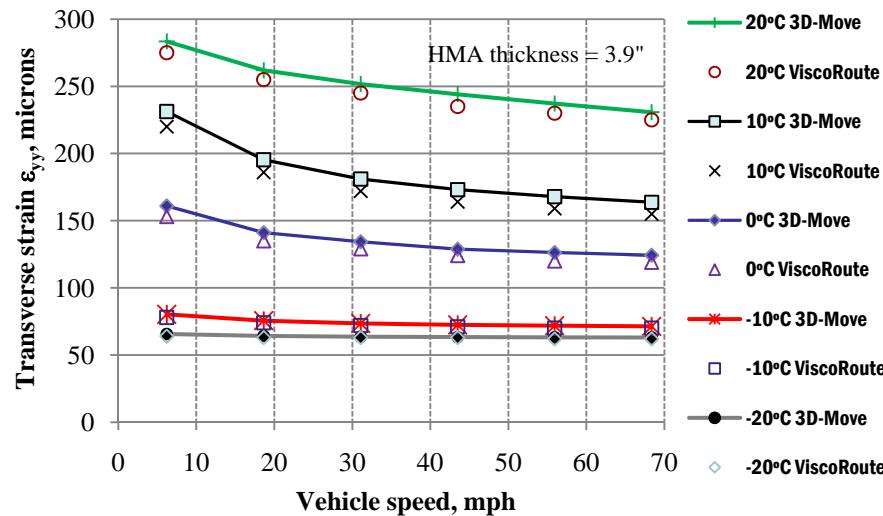
Loft A., "Evaluation de Viscoroute-v1 pour l'étude de quelques chaussées souples", Msc.
Dissertation, Dresden University of Technology speciality
Urban and Road construction,
2005.



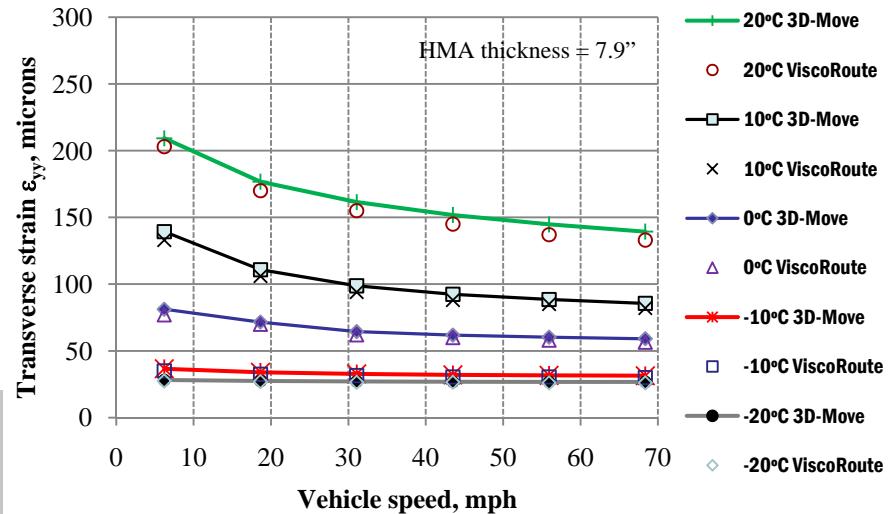
Comparison between elastic computations, ViscoRoute 1.0 simulations and transversal strain measurements at the bottom of bituminous layers for a 4-wheels moving load

Pavement Analysis

3D-Move Analysis Software - Validation



3D-Move vs. ViscoRoute
Vehicle speed = 6 to 70 mph
Pavement temperature = -20°C to 20°C



ViscoRoute Test Results Refer to:

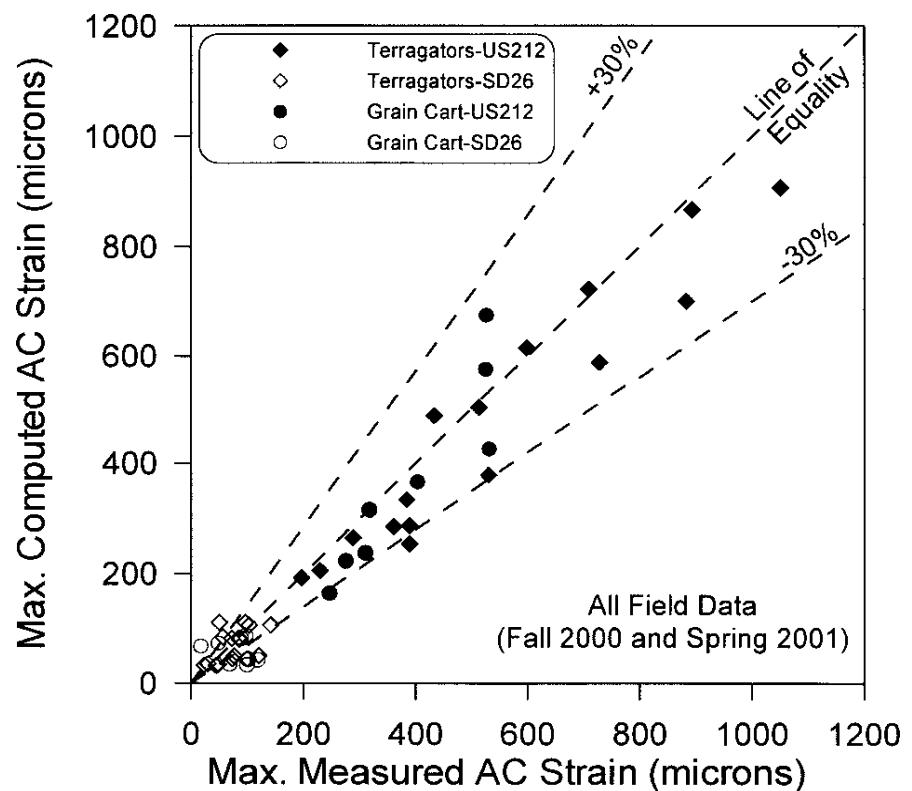
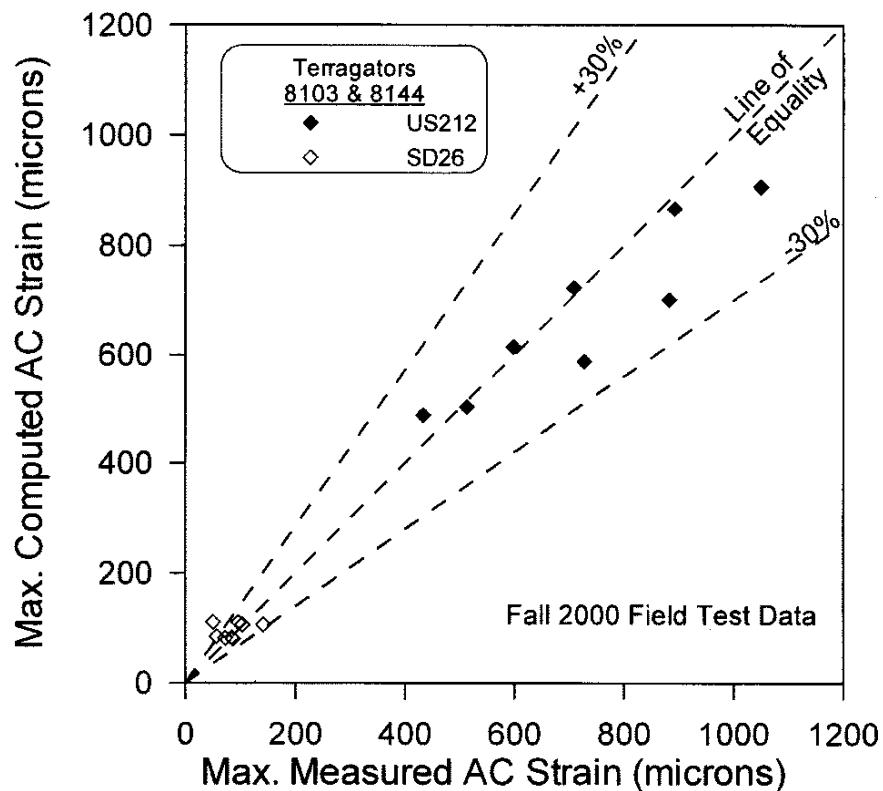
Chabot, A., Chupin, O., Deloffre, L., and Duhamel, D., "Viscoroute 2.0: a tool for the simulation of moving load effects on asphalt pavement," Road Materials and Pavement Design an International Journal, Volume 11/2, 2010, pp. 227-250.

Pavement Analysis

3D-Move Analysis Software - Validation



2. SD Heavy Off-Road Vehicle Field Sections (2000)

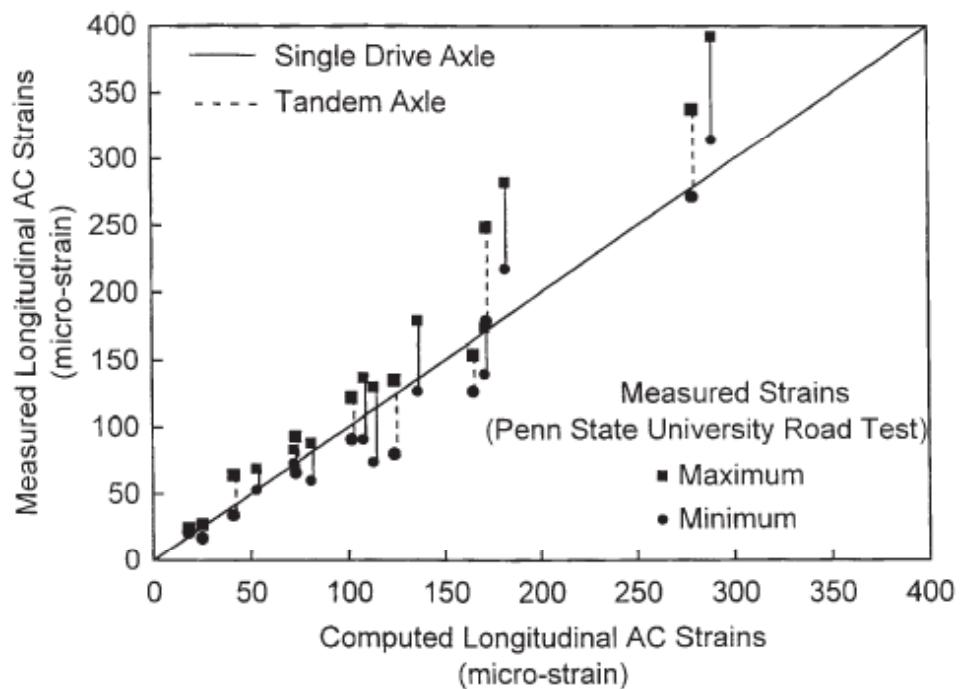
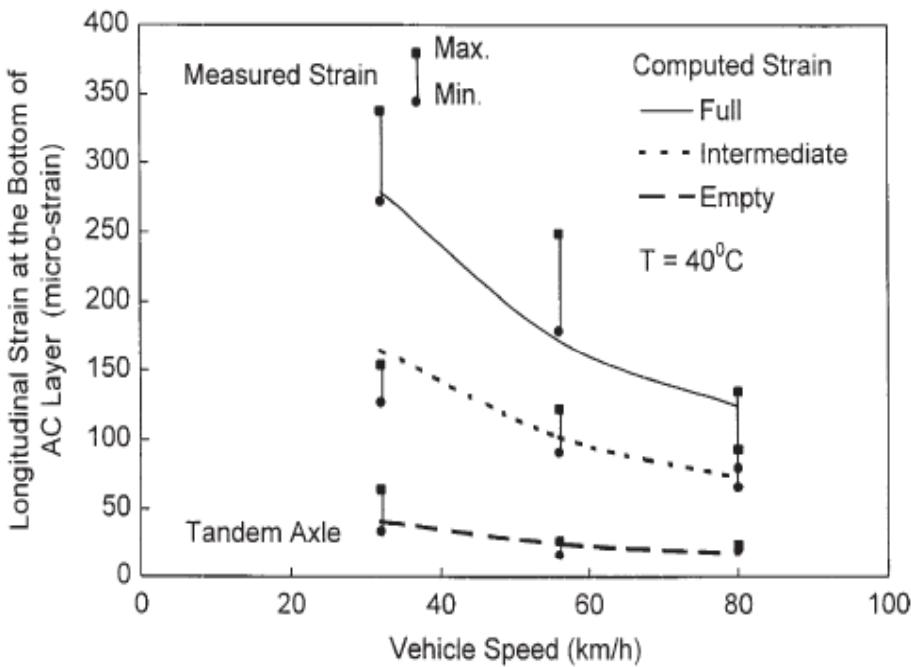


Pavement Analysis

3D-Move Analysis Software - Validation



3. PennState University Test Track (1999)

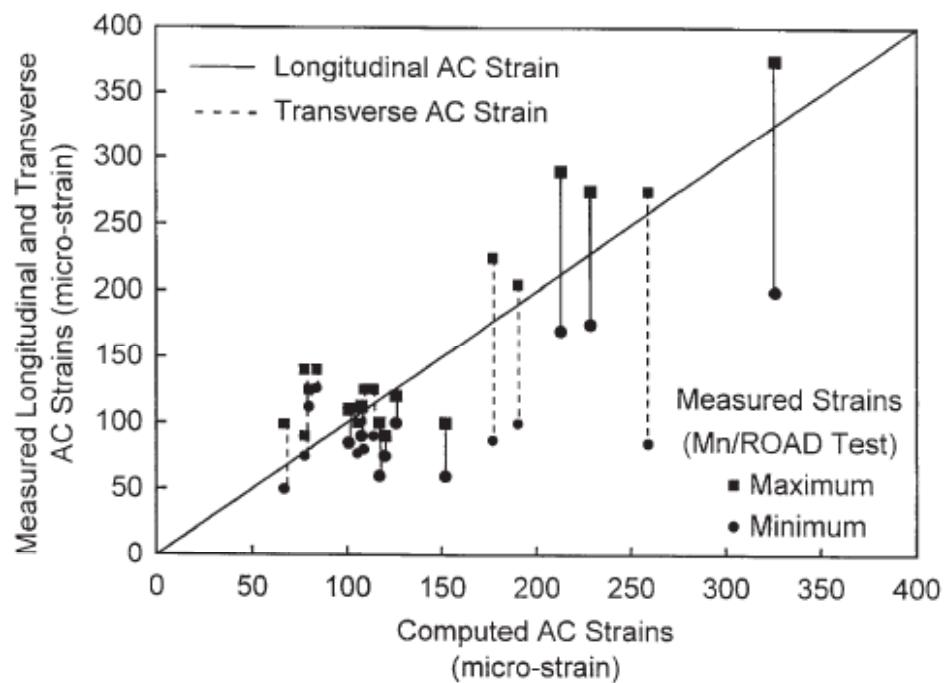
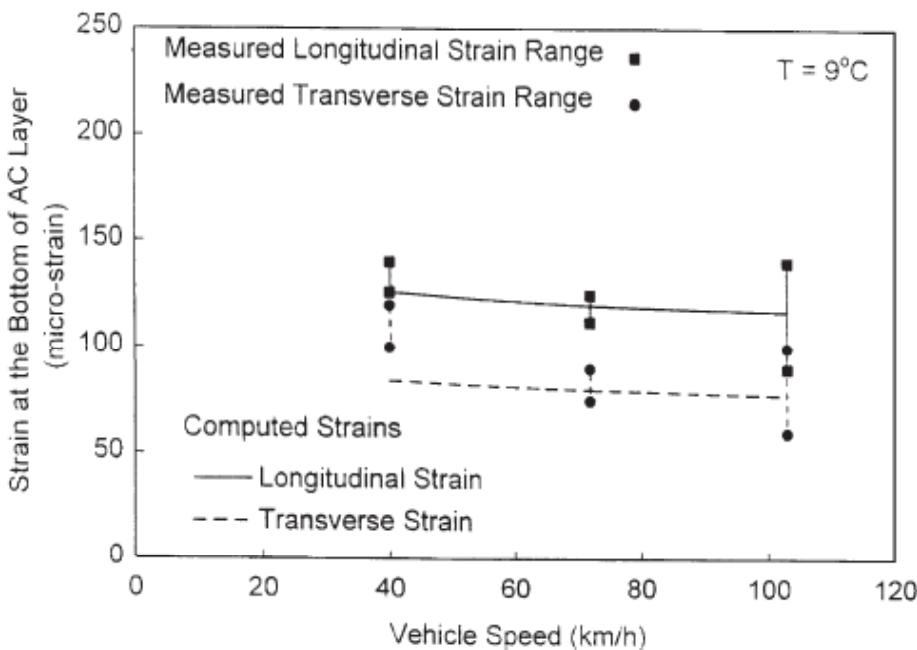


Pavement Analysis

3D-Move Analysis Software - Validation



4. MnRoad (1997)



Database of pavement responses



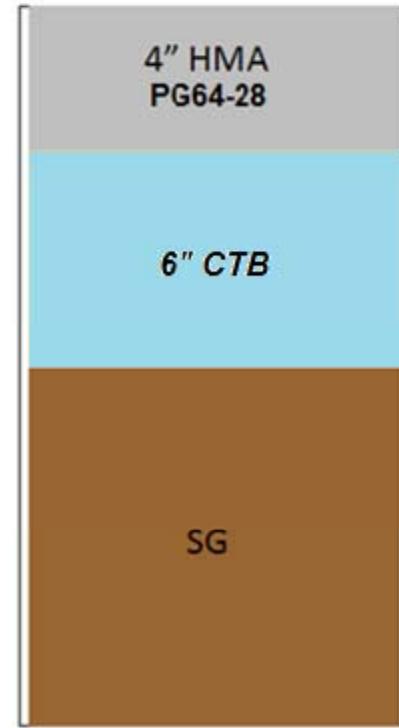
Structure 1



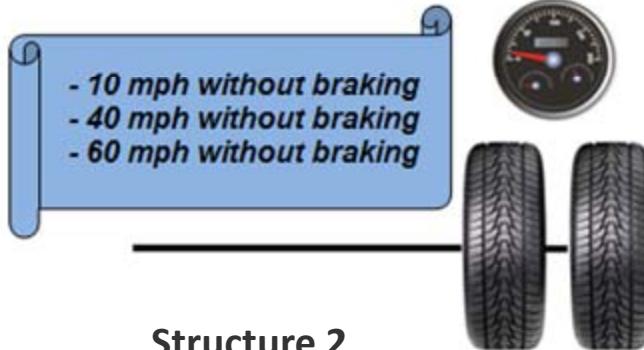
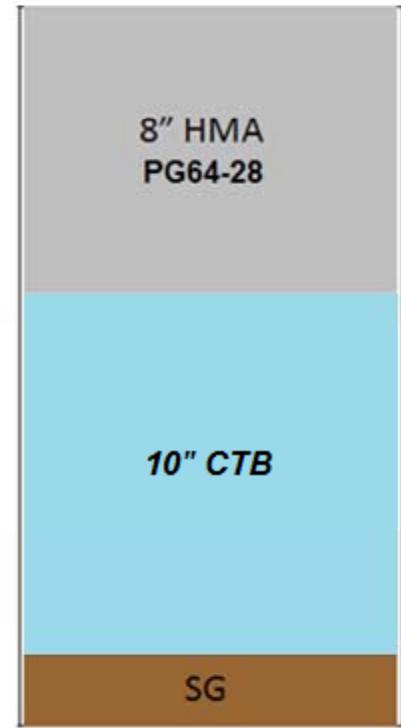
Structure 2



Structure 3



Structure 4



HMA layer temp:
70°F and 104°F

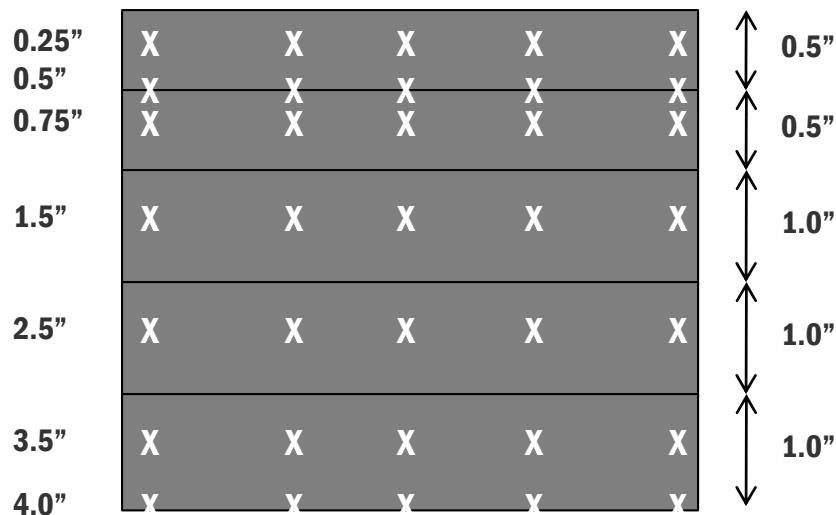


Structures 1 & 2
pavement analyses
completed

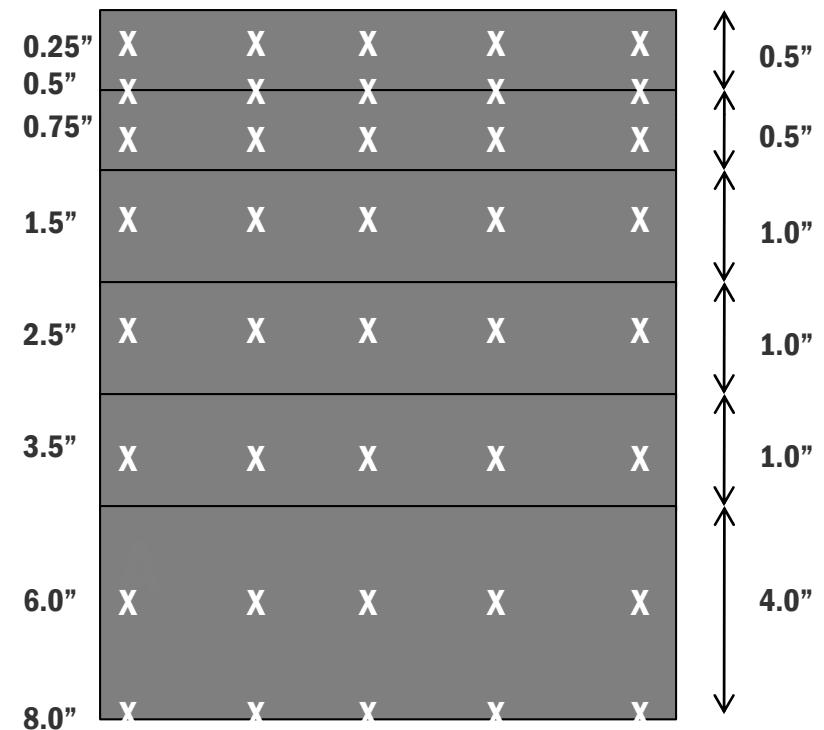
Pavement Responses Locations



4 inch HMA layer



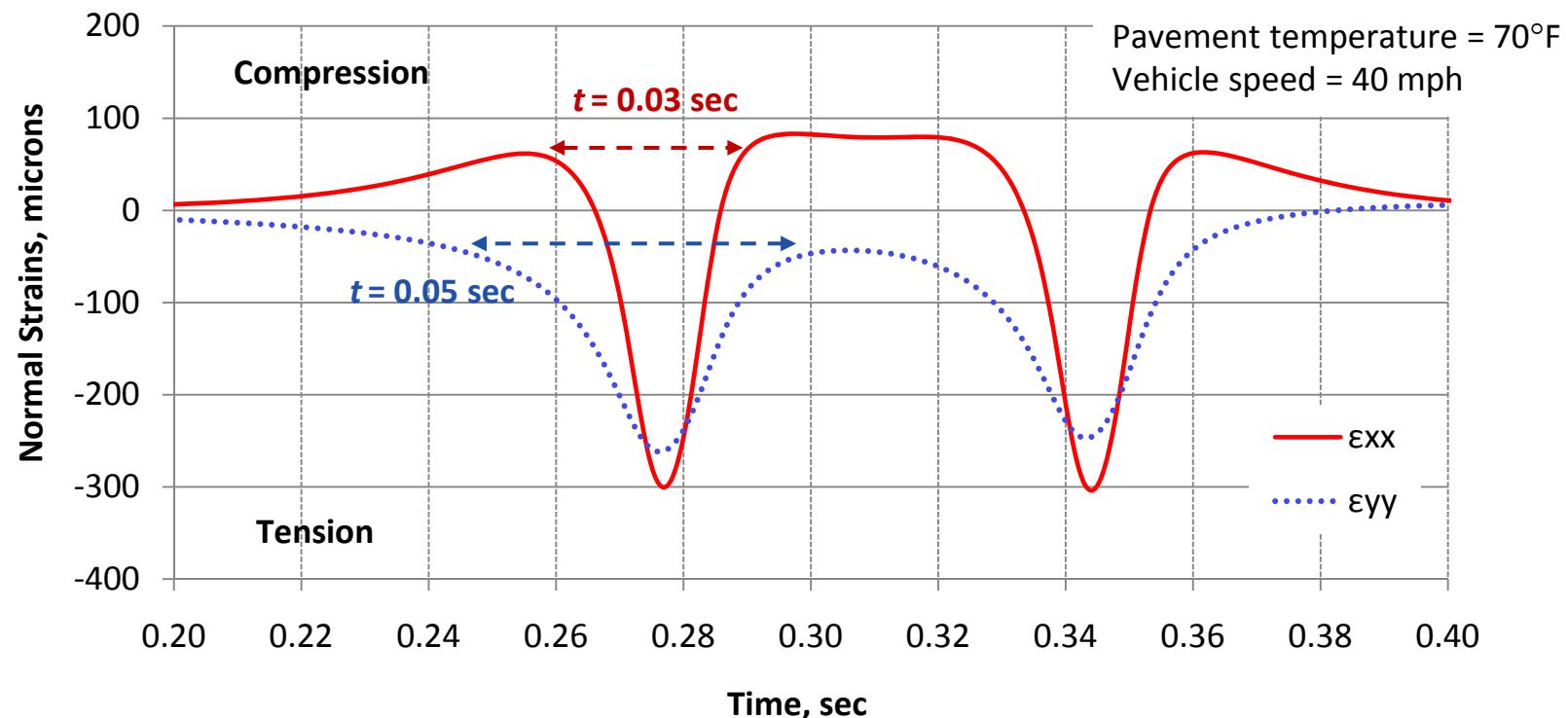
8 inch HMA layer





Proposed approach to determine f_p

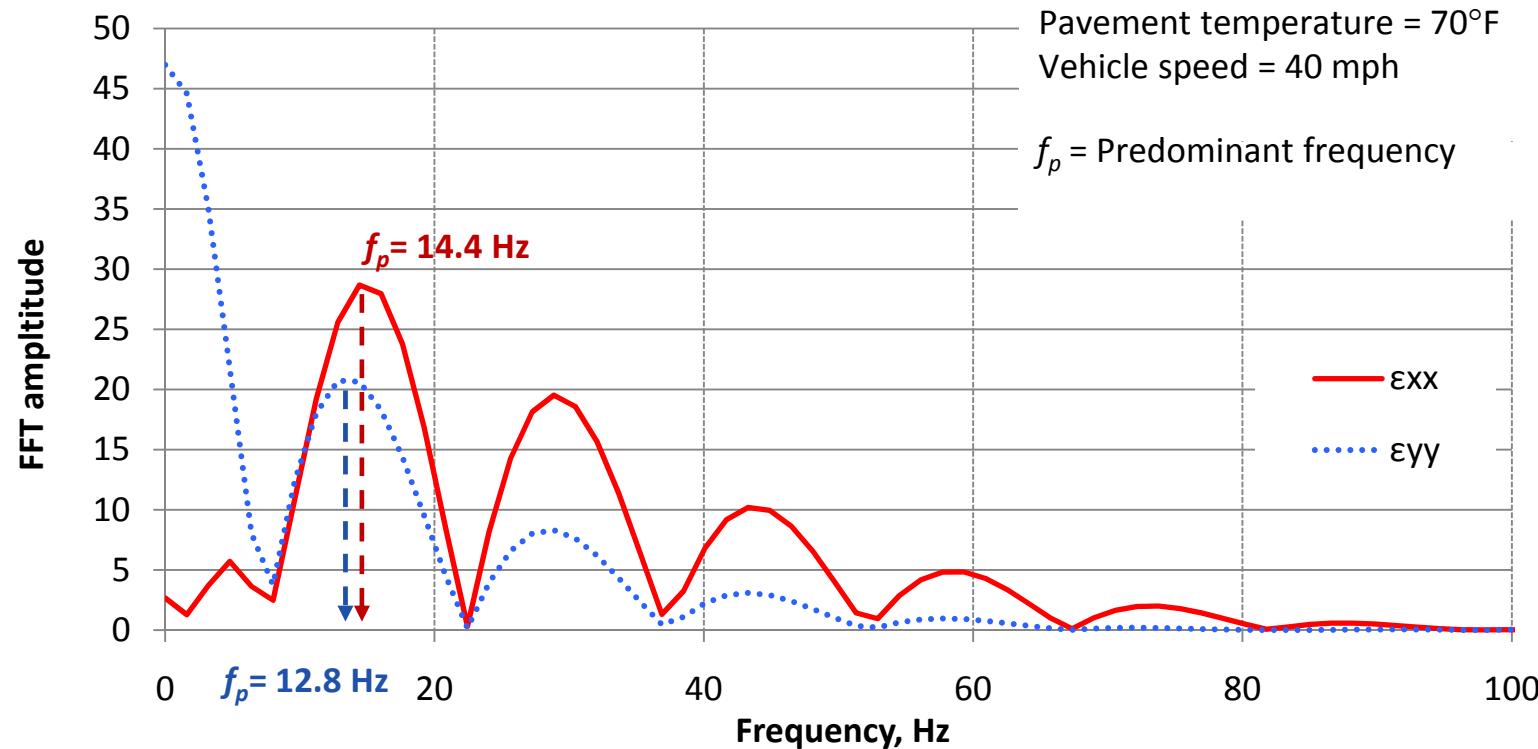
- Example: Bottom of the 4-inch HMA layer:





Proposed approach to determine f_p

- FFT amplitudes of the normal strains of the 4-inch HMA





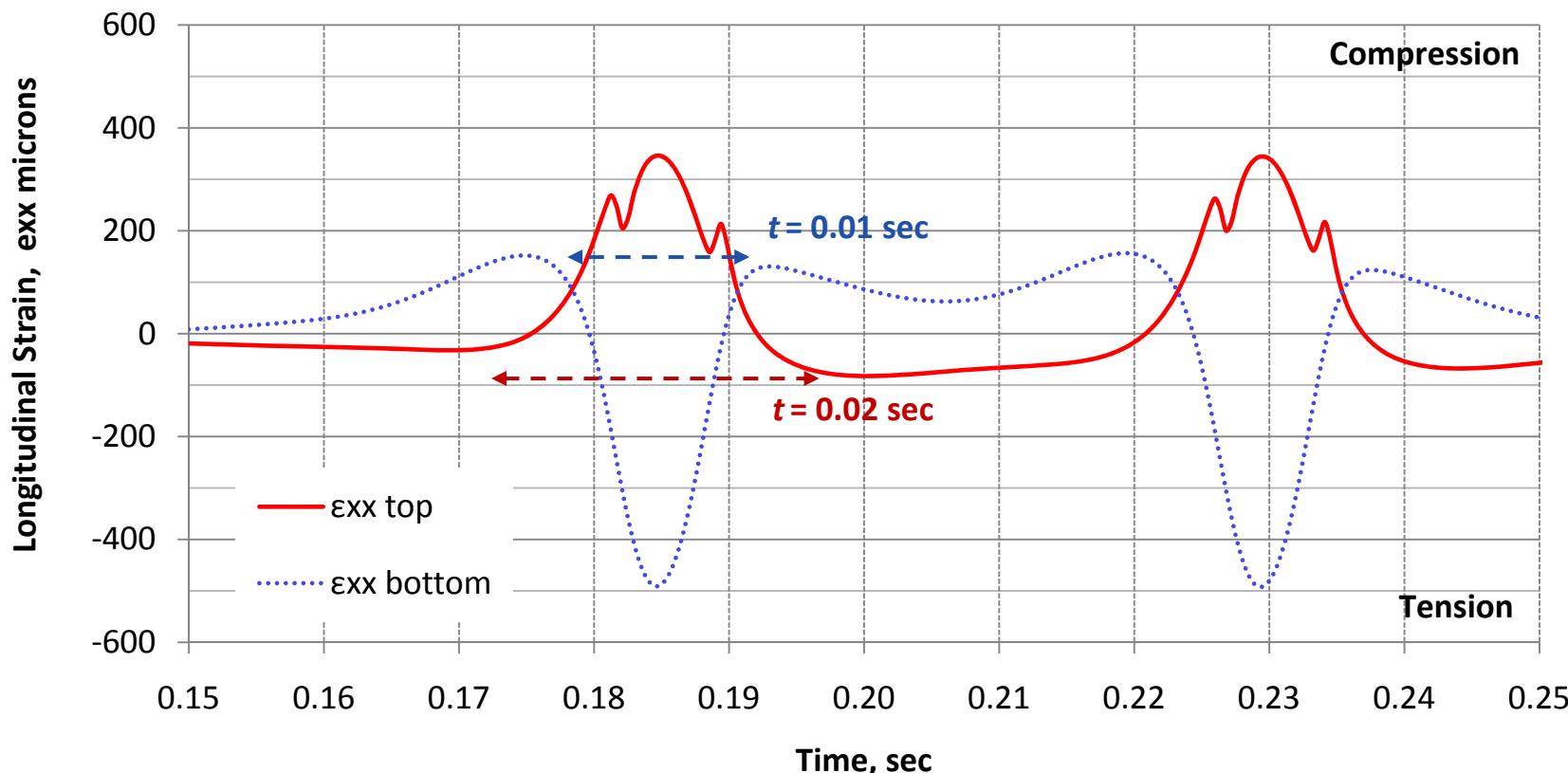
f_p for the 4-inch HMA layer

| Case Study | Depth (in) | Predominant frequency, (Hz) | | | | | | | |
|--------------------------|------------|-----------------------------|--------------|-----------------|--------------|-----------------|--------------|---------------|--------------|
| | | ϵ_{xx} | | ϵ_{yy} | | ϵ_{zz} | | σ_{zz} | |
| | | f_p | f_{pseudo} | f_p | f_{pseudo} | f_p | f_{pseudo} | f_p | f_{pseudo} |
| Case 1: 70°F and 40 mph | 0.25 | 14.4 | 14.4 | 12.8 | 14.4 | 14.4 | 14.4 | 14.4 | 14.4 |
| | 0.5 | 14.4 | | 12.8 | | 14.4 | | 14.4 | |
| | 0.75 | 14.4 | | 12.8 | | 14.4 | | 14.4 | |
| | 1.5 | 14.4 | | 12.8 | | 14.4 | | 14.4 | |
| | 2.5 | 14.4 | | 12.8 | | 14.4 | | 14.4 | |
| | 3.5 | 14.4 | | 12.8 | | 14.4 | | 14.4 | |
| | 4 | 14.4 | | 12.8 | | 14.4 | | 14.4 | |
| Case 2: 104°F and 40 mph | 0.25 | 14.4 | 14.4 | 14.4 | 14.4 | 14.4 | 30.4 | 14.4 | 14.4 |
| | 0.5 | 14.4 | | 12.8 | | 30.4 | | 14.4 | |
| | 0.75 | 14.4 | | 14.4 | | 30.4 | | 14.4 | |
| | 1.5 | 12.8 | | 14.4 | | 30.4 | | 14.4 | |
| | 2.5 | 30.4 | | 14.4 | | 14.4 | | 14.4 | |
| | 3.5 | 30.4 | | 14.4 | | 14.4 | | 14.4 | |
| | 4 | 28.8 | | 14.4 | | 14.4 | | 14.4 | |
| Case 3: 70°F and 60 mph | 0.25 | 21.6 | 21.6 | 19.4 | 21.6 | 21.6 | 21.6 | 21.6 | 21.6 |
| | 0.5 | 21.6 | | 19.4 | | 21.6 | | 21.6 | |
| | 0.75 | 21.6 | | 19.4 | | 19.4 | | 21.6 | |
| | 1.5 | 21.6 | | 16.8 | | 21.6 | | 21.6 | |
| | 2.5 | 21.6 | | 21.6 | | 21.6 | | 21.6 | |
| | 3.5 | 21.6 | | 19.4 | | 21.6 | | 21.6 | |
| | 4 | 21.6 | | 19.4 | | 21.6 | | 21.6 | |
| Case 4: 104°F and 60 mph | 0.25 | 21.6 | 21.6 | 21.6 | 21.6 | 43.3 | 21.6 | 21.6 | 21.6 |
| | 0.5 | 21.6 | | 19.2 | | 43.3 | | 21.6 | |
| | 0.75 | 21.6 | | 19.2 | | 43.3 | | 21.6 | |
| | 1.5 | 21.6 | | 21.6 | | 43.3 | | 21.6 | |
| | 2.5 | 43.3 | | 21.6 | | 21.6 | | 21.6 | |
| | 3.5 | 43.3 | | 21.6 | | 21.6 | | 21.6 | |
| | 4 | 43.3 | | 21.6 | | 21.6 | | 21.6 | |
| Case 5: 70°F and 10 mph | 0.25 | 3.6 | 7.6 | 3.2 | 3.6 | 3.6 | 7.6 | 3.6 | 3.6 |
| | 0.5 | 3.6 | | 3.2 | | 3.6 | | 3.6 | |
| | 0.75 | 3.6 | | 3.2 | | 3.6 | | 3.6 | |
| | 1.5 | 3.2 | | 3.2 | | 7.6 | | 3.6 | |
| | 2.5 | 7.6 | | 3.6 | | 7.6 | | 3.6 | |
| | 3.5 | 4 | | 3.6 | | 3.6 | | 3.6 | |
| | 4 | 4 | | 3.6 | | 3.6 | | 3.6 | |
| Case 6: 104°F and 10 mph | 0.25 | 7.6 | 11.2 | 3.2 | 3.6 | 7.6 | 7.6 | 3.6 | 3.6 |
| | 0.5 | 7.6 | | 3.2 | | 7.6 | | 3.6 | |
| | 0.75 | 7.6 | | 3.2 | | 7.6 | | 3.6 | |
| | 1.5 | 11.2 | | 3.6 | | 3.6 | | 3.6 | |
| | 2.5 | 11.2 | | 3.6 | | 3.6 | | 3.6 | |
| | 3.5 | 11.2 | | 3.6 | | 3.6 | | 3.6 | |
| | 4 | 11.2 | | 3.6 | | 3.6 | | 3.6 | |



Case 4 Predominant Frequencies

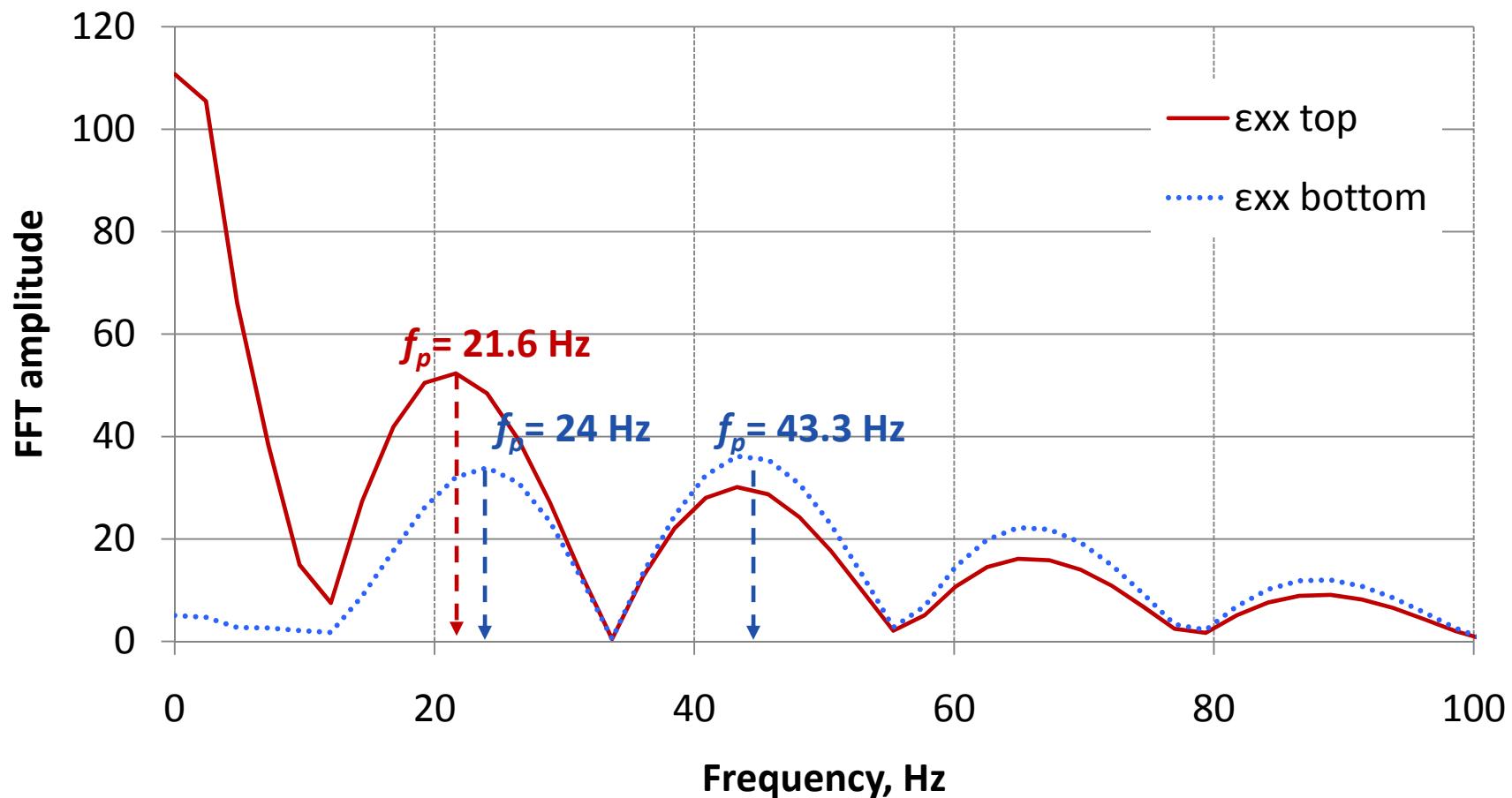
Temp = 104°F, V = 60 mph, Tensile Strain ϵ_{xx}



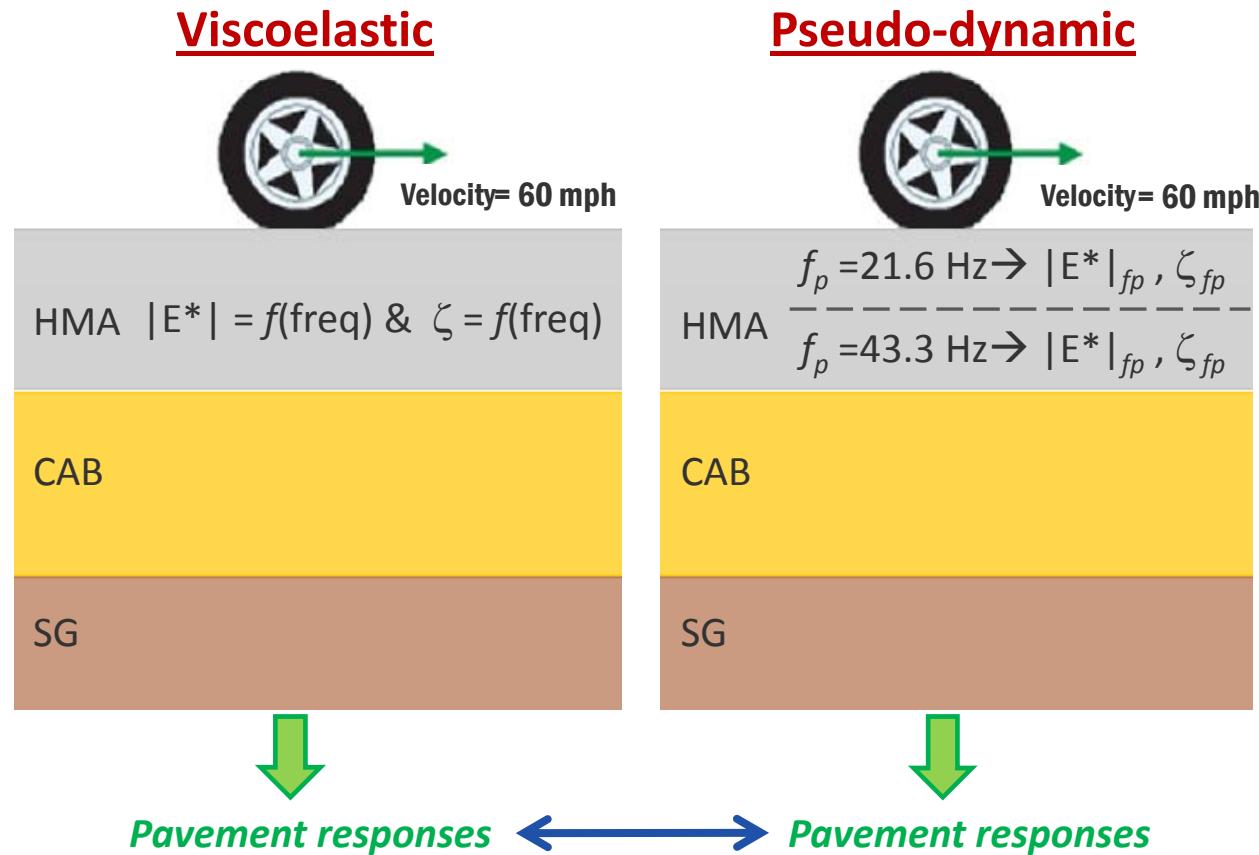


Case 4 Predominant Frequencies

Temp = 104°F, V = 60 mph, Tensile Strain ε_{xx}



Pseudo-Dynamic Analysis

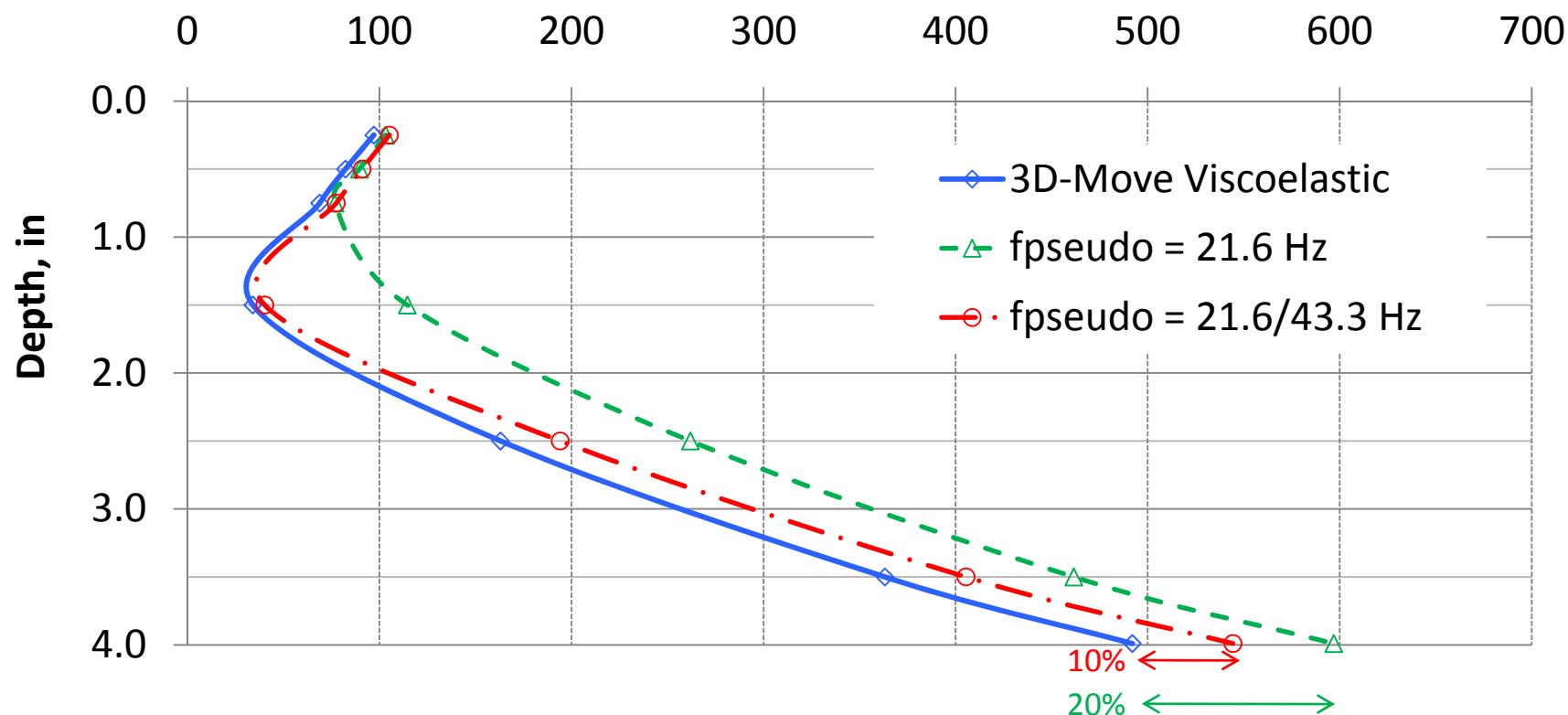




Case 4 Pseudo-Dynamic Analysis

Temp = 104°F, V = 60 mph, Tensile Strain ε_{xx}

Maximum tensile strain ε_{xx} , microns





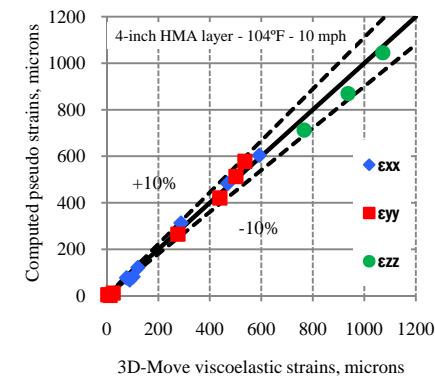
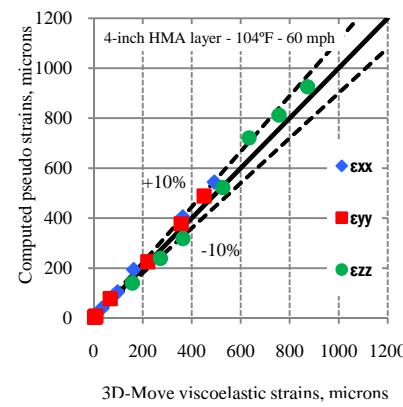
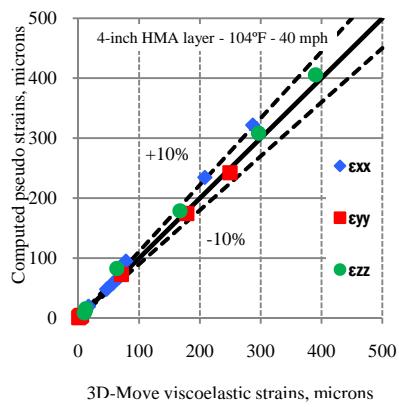
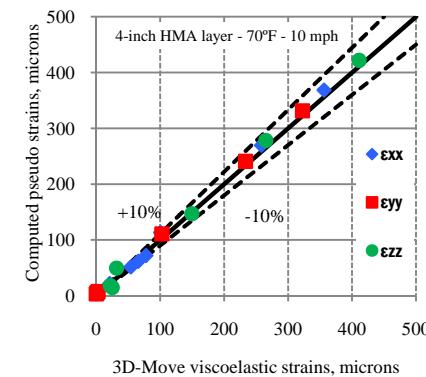
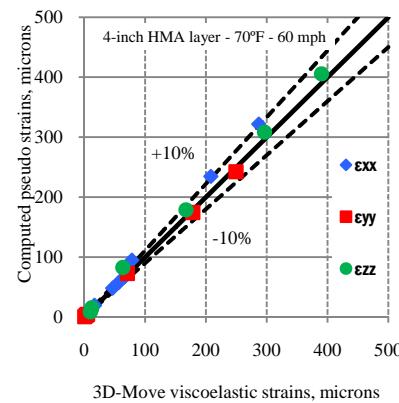
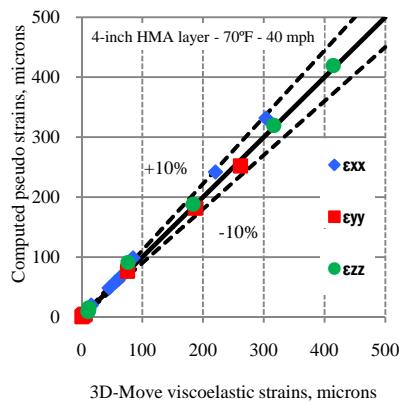
f_p for the 8-inch HMA layer

| Case Study | Depth* (in) | Predominant frequency, (Hz) | | | | | | | |
|---------------------------|-------------|-----------------------------|--------------|-----------------|--------------|-----------------|--------------|---------------|--------------|
| | | ϵ_{xx} | | ϵ_{yy} | | ϵ_{zz} | | σ_{zz} | |
| | | f_p | f_{pseudo} | f_p | f_{pseudo} | f_p | f_{pseudo} | f_p | f_{pseudo} |
| Case 7: 70°F and 40 mph | 0.25 | 12.8 | 12.8 | 16 | 12.8 | 30.4 | 30.4 | 14.4 | 14.4 |
| | 0.5 | 12.8 | | 11.2 | | 30.4 | | 14.4 | |
| | 0.75 | 12.8 | | 9.6 | | 30.4 | | 14.4 | |
| | 1.5 | 12.8 | | 14.4 | | 30.4 | | 14.4 | |
| | 2.5 | 12.8 | | 14.4 | | 30.4 | | 14.4 | |
| | 3.5 | 30.4 | | 14.4 | | 14.4 | | 14.4 | |
| | 6 | 30.4 | | 12.8 | | 12.8 | | 14.4 | |
| | 8 | 14.4 | | 12.8 | | 12.8 | | 14.4 | |
| Case 8: 104°F and 40 mph | 0.25 | 14.4 | 14.4 | 12.8 | 14.4 | 30.4 | 30.4 | 14.4 | 14.4 |
| | 0.5 | 14.4 | | 12.8 | | 30.4 | | 14.4 | |
| | 0.75 | 14.4 | | 11.2 | | 30.4 | | 14.4 | |
| | 1.5 | 12.8 | | 12.8 | | 30.4 | | 14.4 | |
| | 2.5 | 30.4 | | 12.8 | | 14.4 | | 14.4 | |
| | 3.5 | 30.4 | | 12.8 | | 14.4 | | 14.4 | |
| | 6 | 30.4 | | 12.8 | | 14.4 | | 14.4 | |
| | 8 | 30.4 | | 12.8 | | 14.4 | | 14.4 | |
| Case 9: 70°F and 60 mph | 0.25 | 19.2 | 19.2 | 19.2 | 19.2 | 19.2 | 45.7 | 21.6 | 21.6 |
| | 0.5 | 19.2 | | 16.8 | | 40.8 | | 21.6 | |
| | 0.75 | 19.2 | | 16.8 | | 45.7 | | 21.6 | |
| | 1.5 | 19.2 | | 19.2 | | 45.7 | | 21.6 | |
| | 2.5 | 19.2 | | 19.2 | | 43.2 | | 21.6 | |
| | 3.5 | 45.7 | | 21.6 | | 21.6 | | 21.6 | |
| | 6 | 45.7 | | 19.2 | | 19.2 | | 21.6 | |
| | 8 | 45.7 | | 19.2 | | 19.2 | | 21.6 | |
| Case 10: 104°F and 60 mph | 0.25 | 21.6 | 21.6 | 19.2 | 21.6 | 45.7 | 45.7 | 21.6 | 21.6 |
| | 0.5 | 21.6 | | 19.2 | | 45.7 | | 21.6 | |
| | 0.75 | 19.2 | | 16.8 | | 45.7 | | 21.6 | |
| | 1.5 | 45.7 | | 21.6 | | 21.6 | | 21.6 | |
| | 2.5 | 45.7 | | 21.6 | | 21.6 | | 21.6 | |
| | 3.5 | 43.3 | | 21.6 | | 21.6 | | 21.6 | |
| | 6 | 43.3 | | 21.6 | | 21.6 | | 21.6 | |
| | 8 | 43.3 | | 19.2 | | 21.6 | | 21.6 | |
| Case 11: 70°F and 10 mph | 0.25 | 3.6 | 3.6 | 3.2 | 3.6 | 7.6 | 7.6 | 3.6 | 3.6 |
| | 0.5 | 3.6 | | 3.2 | | 7.6 | | 3.6 | |
| | 0.75 | 3.6 | | 3.2 | | 7.6 | | 3.6 | |
| | 1.5 | 3.6 | | 3.6 | | 7.6 | | 3.6 | |
| | 2.5 | 3.6 | | 3.6 | | 7.6 | | 3.6 | |
| | 3.5 | 7.6 | | 3.6 | | 7.6 | | 3.6 | |
| | 6 | 3.6 | | 3.2 | | 3.6 | | 3.6 | |
| | 8 | 3.6 | | 3.2 | | 3.6 | | 3.2 | |
| Case 12: 104°F and 10 mph | 0.25 | 3.6 | 11.2 | 3.2 | 3.6 | 7.6 | 7.6 | 3.6 | 3.6 |
| | 0.5 | 3.6 | | 3.2 | | 7.6 | | 3.6 | |
| | 0.75 | 3.2 | | 3.6 | | 7.6 | | 3.6 | |
| | 1.5 | 11.2 | | 3.6 | | 3.6 | | 3.6 | |
| | 2.5 | 11.2 | | 3.6 | | 3.6 | | 3.6 | |
| | 3.5 | 11.2 | | 3.6 | | 3.6 | | 3.6 | |
| | 6 | 4 | | 3.2 | | 3.6 | | 3.6 | |
| | 8 | 3.6 | | 3.2 | | 3.6 | | 3.2 | |

Viscoelastic vs. Pseudo-Dynamic analysis



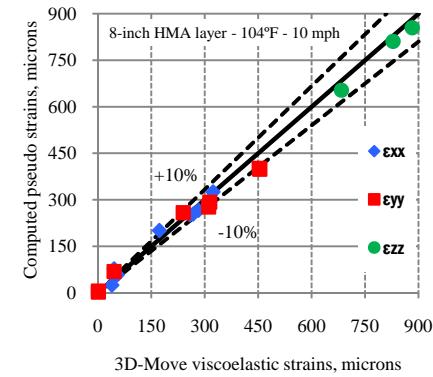
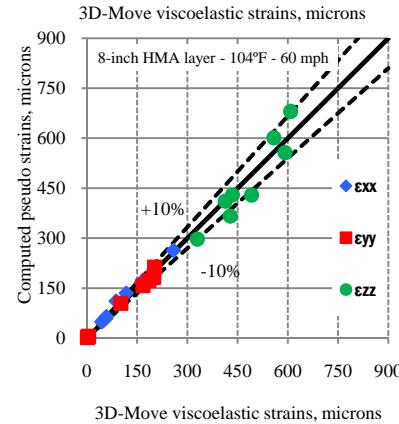
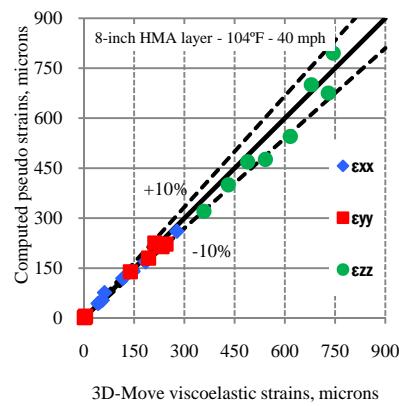
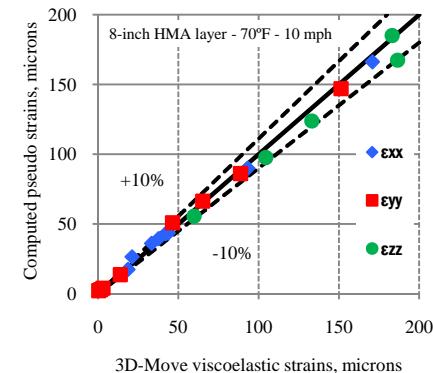
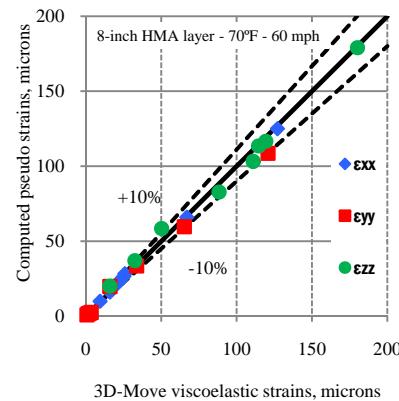
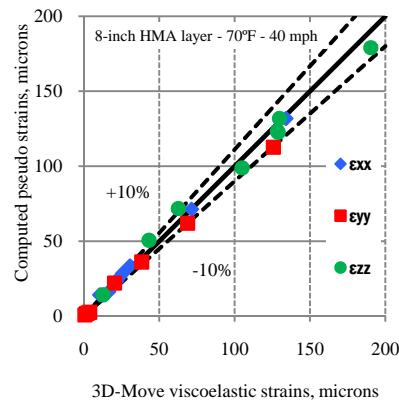
4-inch HMA layer



Viscoelastic vs. Pseudo-Dynamic analysis



8-inch HMA layer





Pseudo-Static Analysis

- Pseudo-Static:
 - Vehicle speed = 0
 - Linear Elastic Analysis (LEA)
 - Use f_p to select $|E^*|_{fp}$
 - Damping $\zeta_{fp} = 0$
- Also Compare pavement responses following
 - MEPDG approach ($f = 1/t$)
 - Modified MEPDG ($f = 1/(2t)$)
 - Ferry ($f = 1/(2\pi t)$)

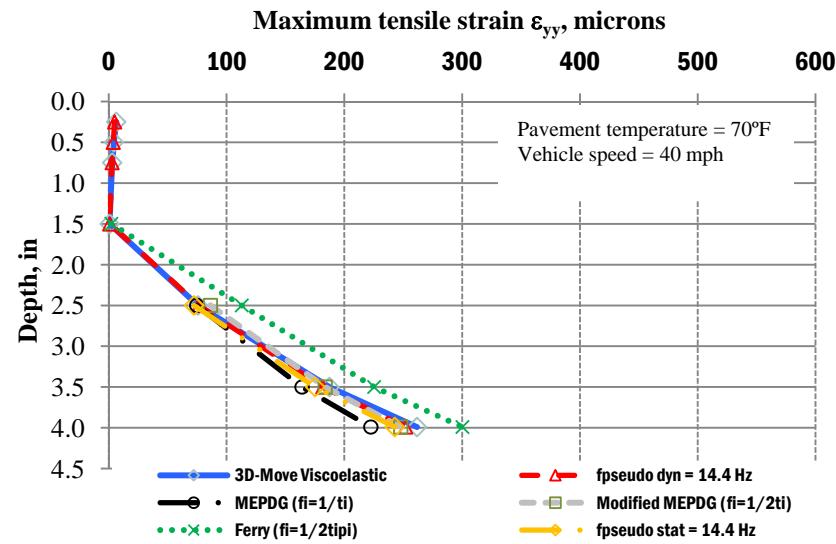
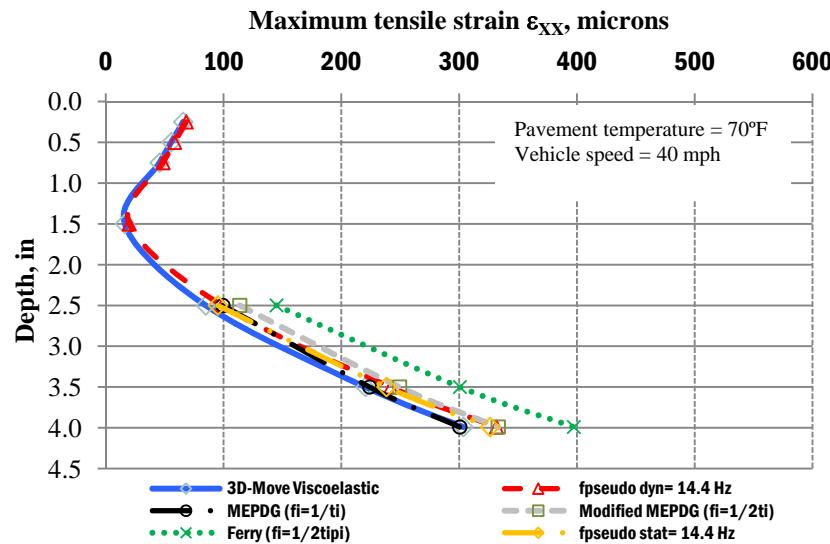


MEPDG Loading Time Calculation

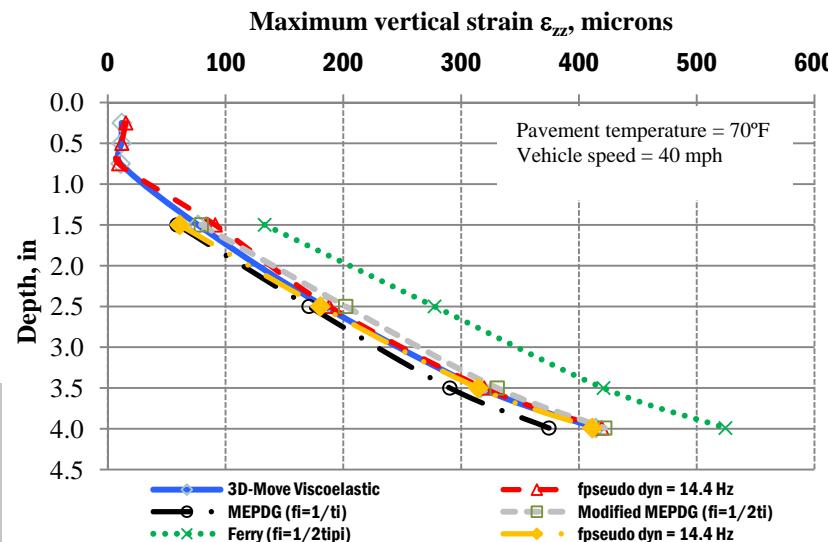
4-inch HMA layer – 70°F and 10 mph

| Sublayer | Thickness (in) | Cummulated Thickness (in) | Z _{eff} (in) | Condition | L _{eff} (in) | t (sec) | f = 1/t (Hz) | E* (psi) |
|----------|----------------|---------------------------|-----------------------|-----------------|-----------------------|---------|--------------|----------|
| 1 | 0.5 | 0.5 | 1.59 | No overlap | 10.7 | 0.061 | 16.4 | 485,868 |
| 2 | 0.5 | 1 | 3.15 | No overlap | 13.8 | 0.078 | 12.8 | 451,966 |
| 3 | 1 | 2 | 6.11 | Partial overlap | 23.1 | 0.131 | 7.6 | 387,689 |
| 4 | 1 | 3 | 8.97 | Partial overlap | 31.3 | 0.178 | 5.6 | 352,161 |
| 5 | 1 | 4 | 11.77 | Partial overlap | 38.9 | 0.221 | 4.5 | 328,345 |

Pavement responses comparison

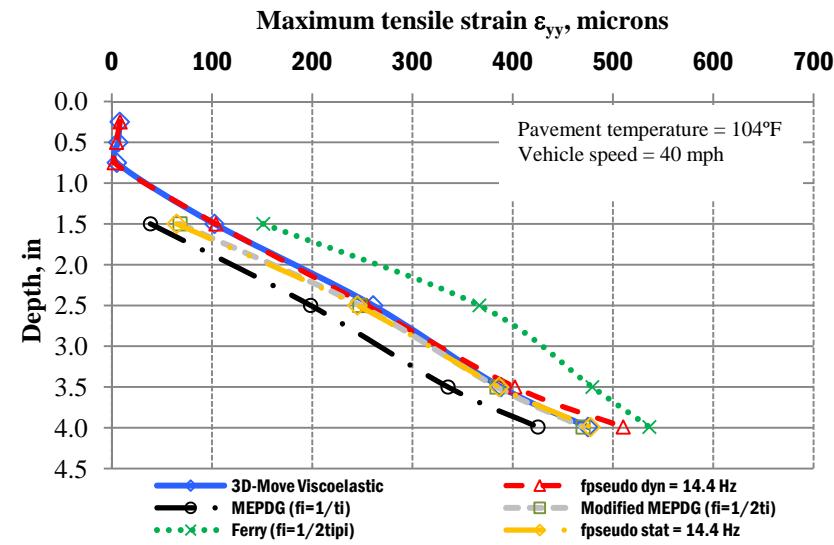
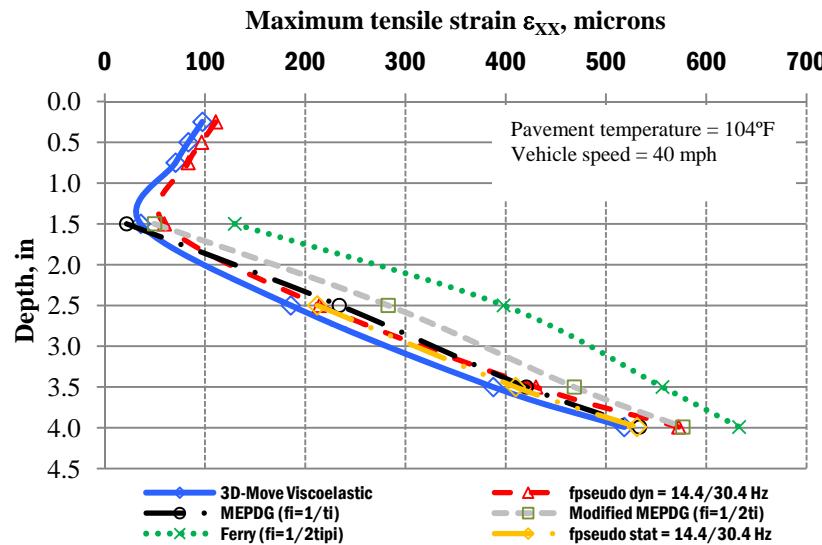


Pavement
temperature = 70 °F
4-inch HMA layer
40 mph

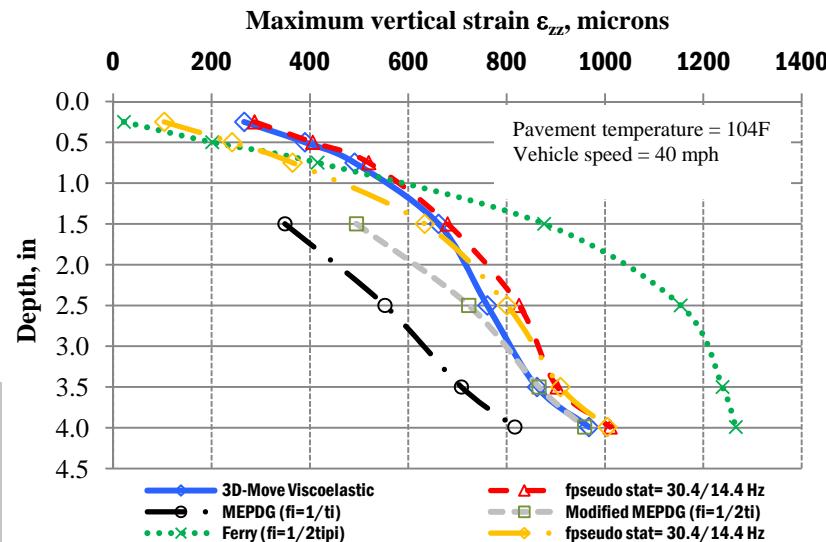




Pavement responses comparison

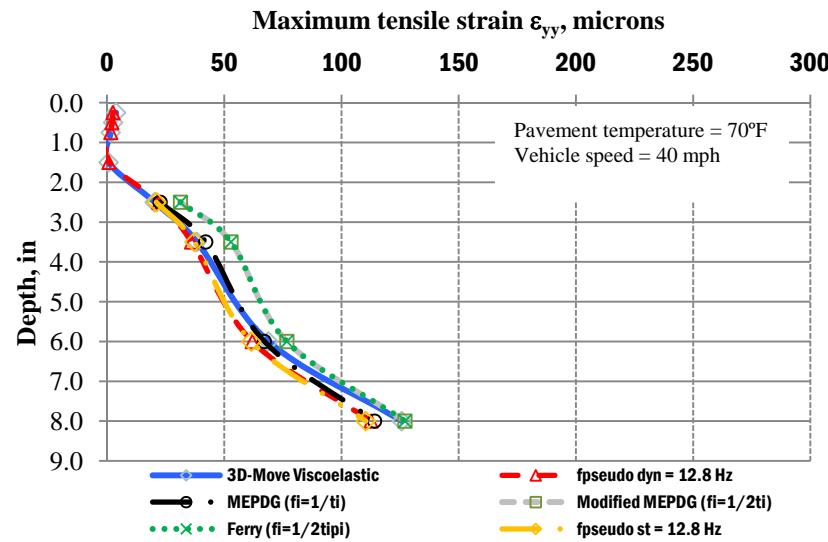
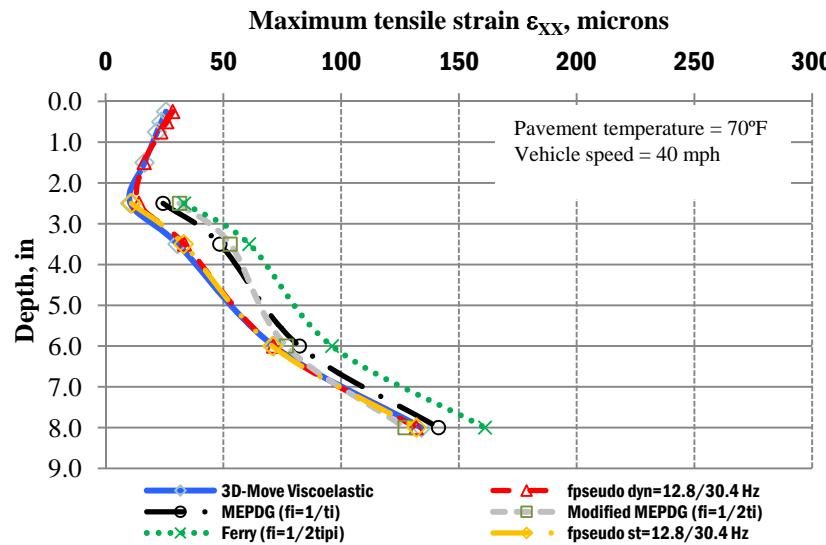


Pavement
temperature = 104 °F
4-inch HMA layer
40 mph

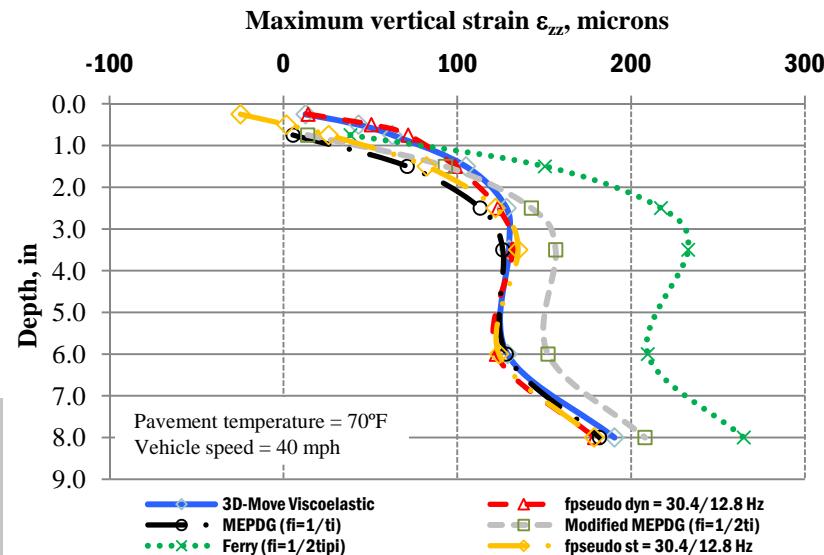




Pavement responses comparison

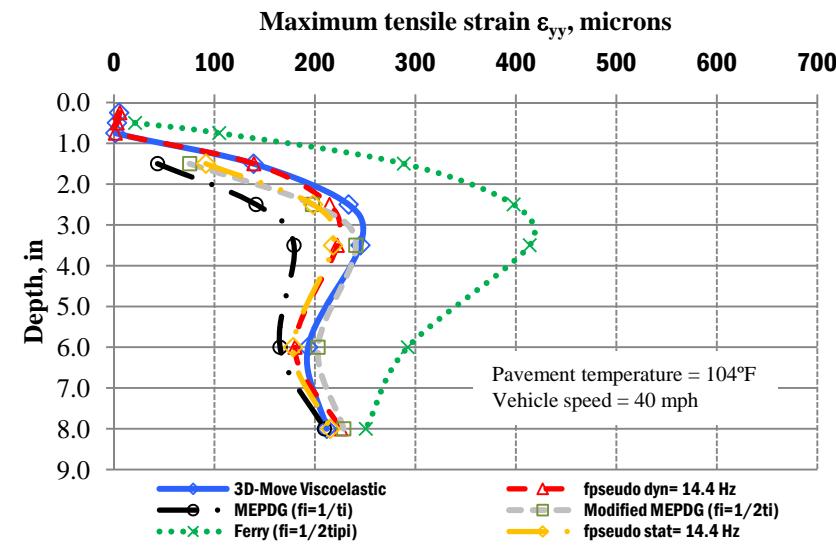
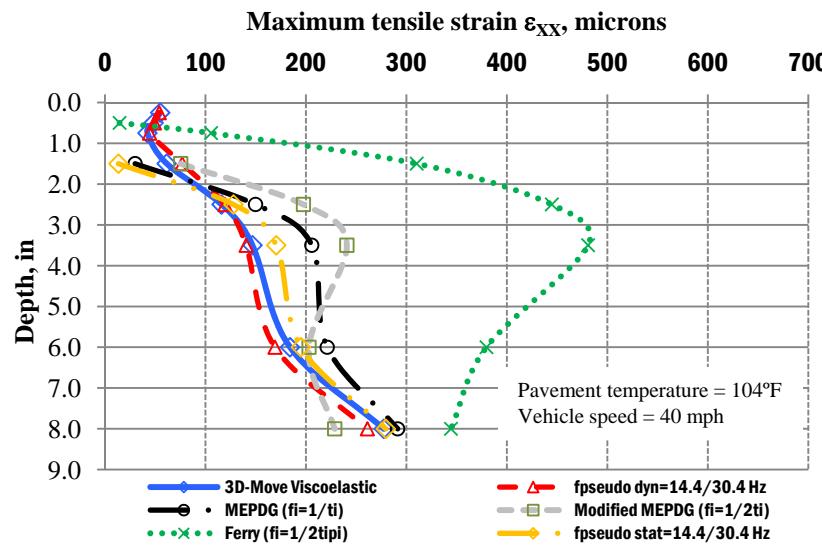


Pavement
temperature = 70 °F
8-inch HMA layer
40 mph

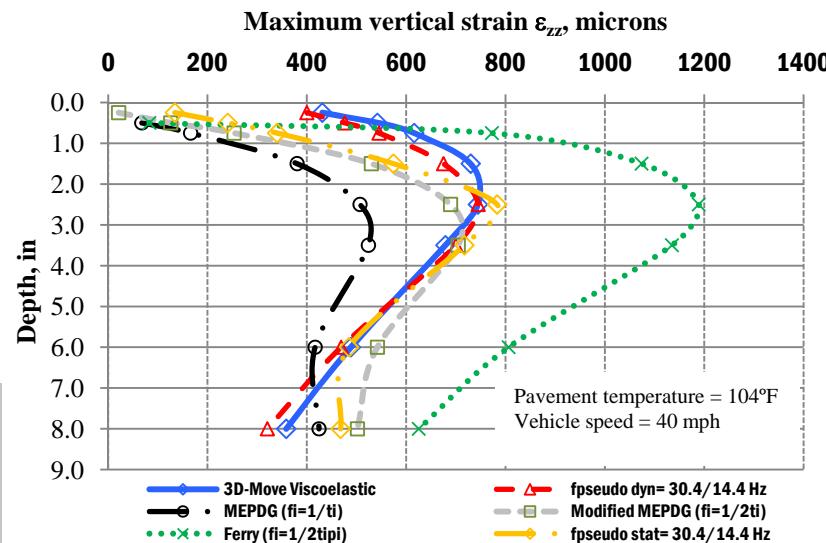




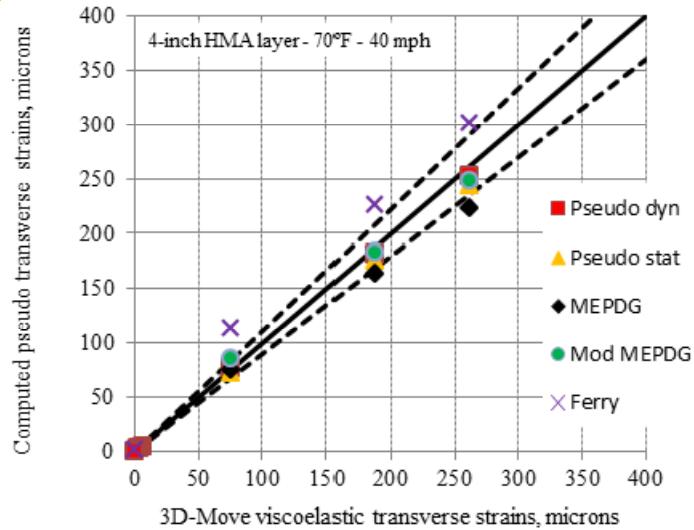
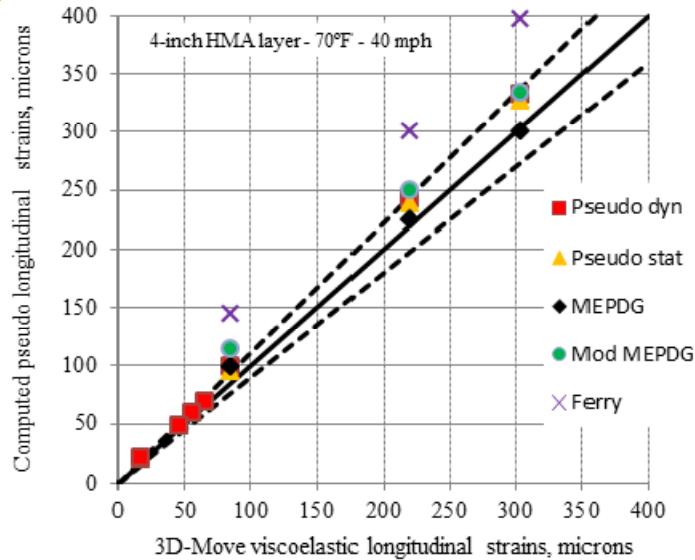
Pavement responses comparison



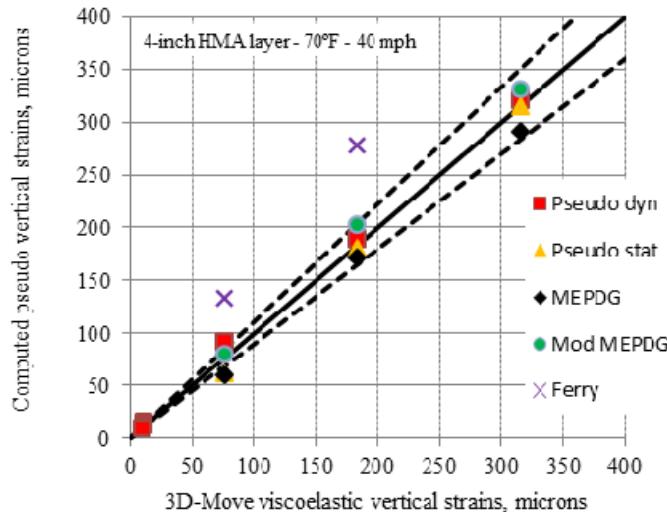
Pavement
temperature = 104 °F
8-inch HMA layer
40 mph



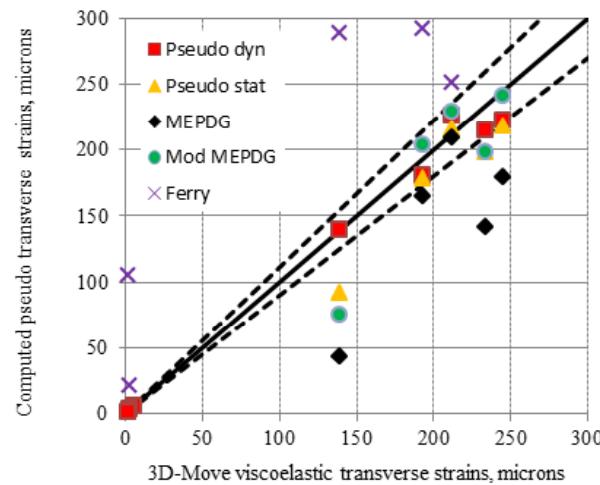
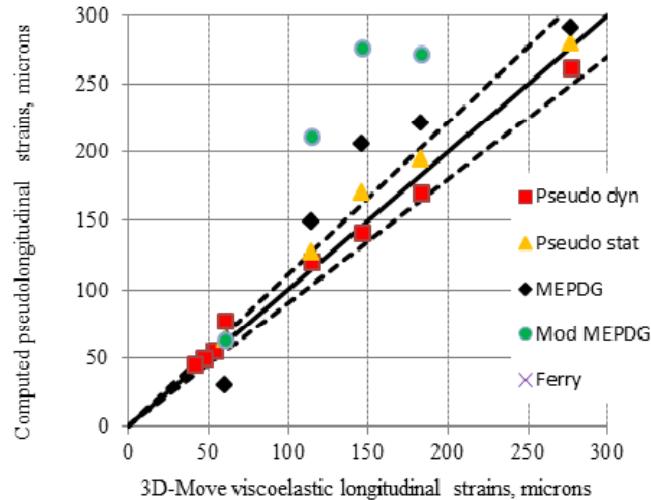
Pavement responses comparison



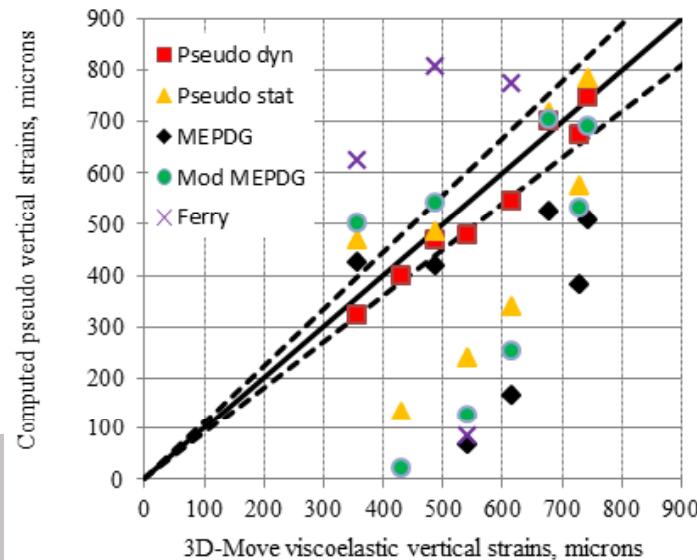
Pavement
temperature = 70 °F
4-inch HMA layer



Pavement responses comparison

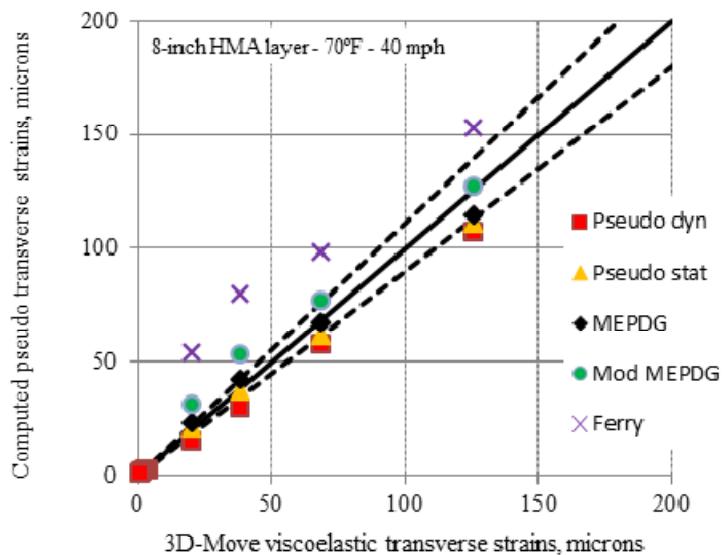
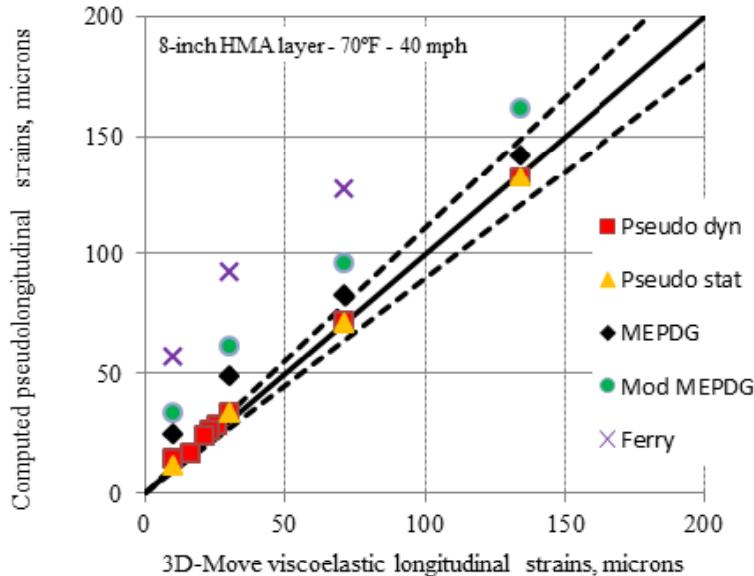


Pavement
temperature = 104 °F
4-inch HMA layer

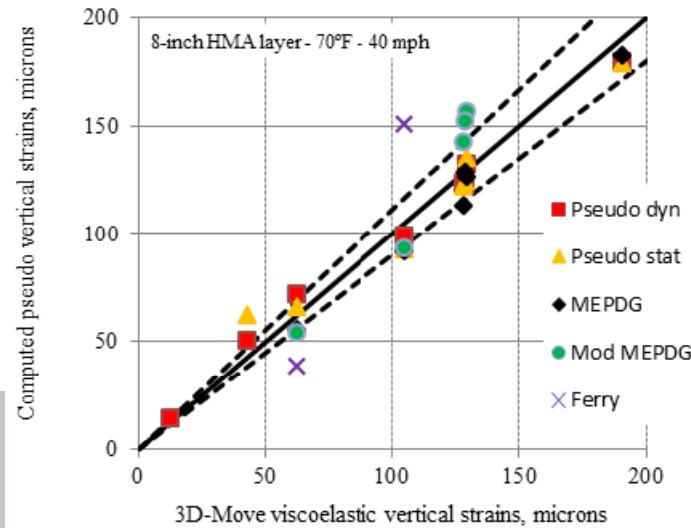




Pavement responses comparison

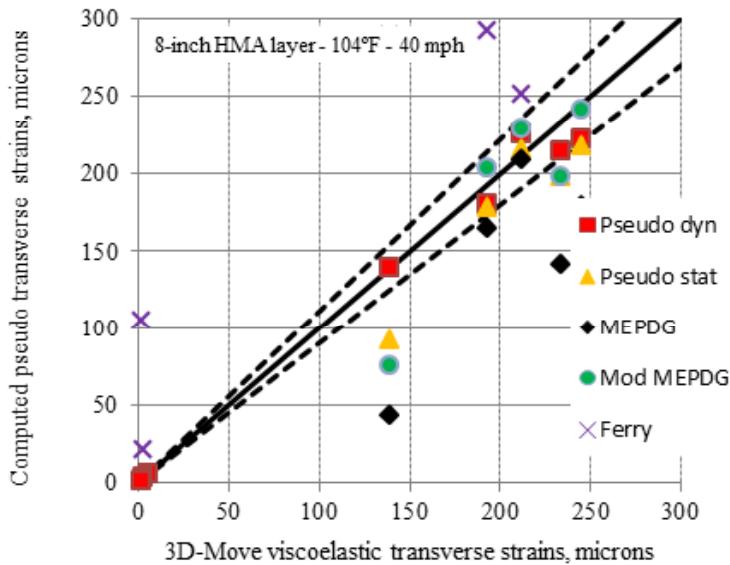
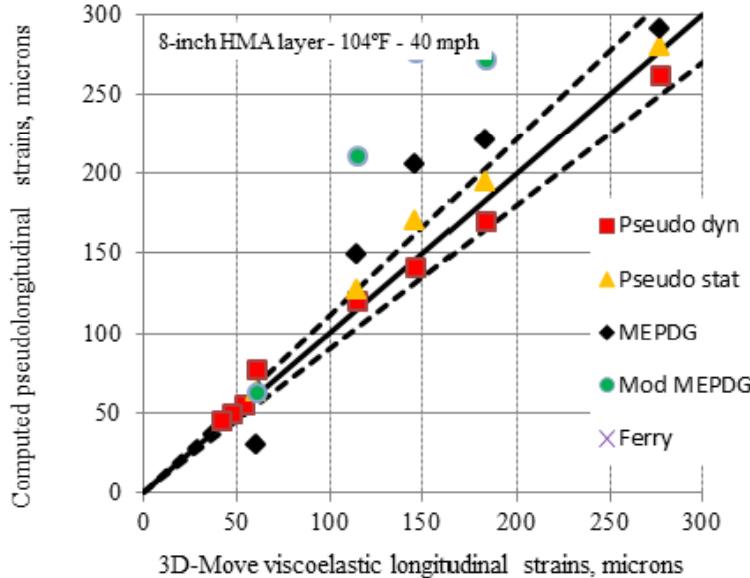


Pavement
temperature = 70 °F
8-inch HMA layer

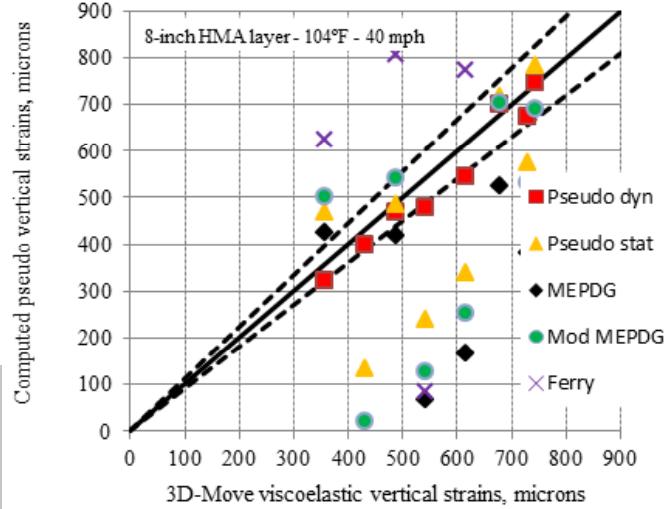




Pavement responses comparison



Pavement
temperature = 104 °F
8-inch HMA layer





Overall Findings

- Use of one single set of f_p cannot be assigned to the AC layer to study all responses.
- Pavement responses can be successfully predicted (within $\pm 10\%$) by *Pseudo-Dynamic* equivalent approach.
- MEPDG approach derives in comparable pavement responses only when asphalt layer is stiff and there are no multiple f_p within the asphalt layer.



Additional needed work...

- Do the analysis at locations other than the center line
- Investigate influence of axle load, response location and axle configuration on f_p .
- Investigate influence of CTB on f_p .
- Evaluate different time-frequency conversions.
- Other!

...Feedback...

Acknowledgment



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- Contents reflect the views of the authors and do not necessarily reflect the official views & policies of FHWA.