

Equivalent Loading Frequencies to Simulate Asphalt Layer Pavement Responses Under Dynamic Traffic Loading

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Phoenix, Arizona
March 18, 2011*

Introduction

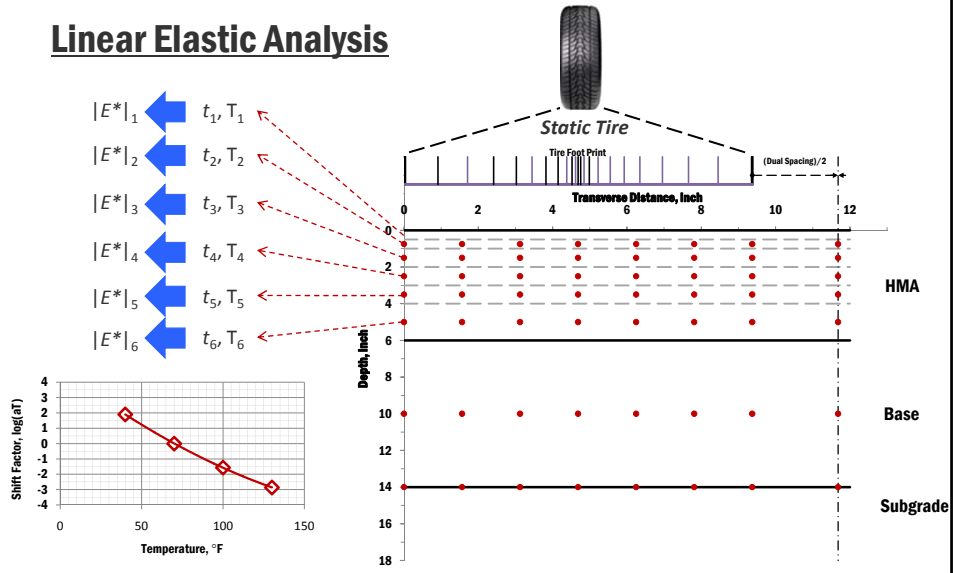


- ***Dynamic response*** of AC pavements under moving load is a key component for accurate prediction of ***flexible pavement performance***.
- ***Reliable determination*** of pavement responses to ***moving load*** is essential for a successful mechanistic design procedure.
- ***Time and temperature dependency*** of asphalt must be considered in the mechanistic analysis response model.

AASHTO MEPDG Approach



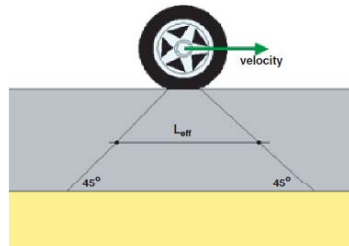
Linear Elastic Analysis



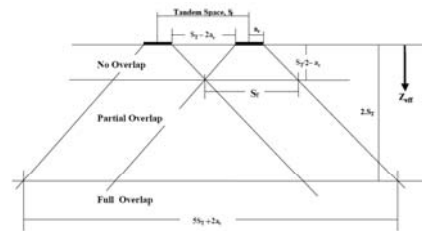
AASHTO MEPDG



- Vertical stress distribution used to estimate traffic-induced loading time.
 - Axle load configuration, Vehicle speed & Pavement structure



$$t = \frac{L_{eff}}{17.6 V_s} \rightarrow f = \frac{1}{t}$$



$$Z_{eff} = \sum_{i=1}^{n-1} \left(h_i \sqrt[3]{\frac{E_i}{E_{SG}}} \right) + h_n \sqrt[3]{\frac{E_n}{E_{SG}}}$$

Literature Review



- Dongre, R. N., Myers, L. A., and D'Angelo, J. A., "Conversion of Testing Frequency to Loading Time: Impact on Performance Predictions Obtained from the Mechanistic–Empirical Pavement Design Guide", Presented at 85th Annual Meeting of the Transportation Research Board, Washington, D.C., 2006.
- Al-Qadi, I. L., W. Xie, and Elseifi, M. A., "Frequency Determination from Vehicular Loading Time Pulse to Predict Appropriate Complex Modulus in MEPDG", Journal of the Association of Asphalt Paving Technologists, Vol. 77, 2008, pp. 739-772.
- Katicha, S., Flintsch, G.W., Loulizi, A., and Wang L. "Conversion of Testing Frequency to Loading Time Applied to Mechanistic-Empirical Pavement Design Guide," Transportation Research Record No. 2087, TRB, Washington D.C., 2008, pp. 99-109.
- ...

Appropriate Representative Elastic Modulus

B. S. Underwood and Y. R. Kim



- "Determination of the Appropriate Representative Elastic Modulus for Asphalt Concrete," IJPE, Vol. 10, Iss. 2, 2009, pp. 77-86
 - Evaluated several approximation methods for calculation of stresses & strains in linear viscoelastic materials.
 - MEPDG method is biased towards overestimating the appropriate stiffness by up to a 31% error.
 - Representative modulus to use for LEA is average of
 - dynamic modulus at a frequency equal to $1/t_p$ and
 - relaxation modulus evaluated at a time equal to $\frac{1}{2} t_p$.
 - Proposed Method resulted in 2 - 6% error

Research Objective



- Investigate the existence of one or more ***predominant frequencies (f_p)*** associated with the AC layer that controls the dynamic response of pavements.
- ***AC Critical Responses:***
 - Longitudinal & transverse tensile strains
 - Vertical compressive strains

Viscoelastic vs. Pseudo Analysis



Viscoelastic



HMA	$ E^* = f(\text{freq})$ & $\zeta = f(\text{freq})$
CAB	
SG	

Pseudo-dynamic



HMA	$ E^* _{f_p} = ?, \zeta_{f_p} = ?$
CAB	
SG	

Pseudo-static



HMA	$ E^* _{f_p} = ? \zeta_{f_p} = 0$
CAB	
SG	

Pavement responses ← ? → Pavement responses ← ? → Pavement responses

Pavement Analysis

3D-Move Analysis Software



Asphalt Research Consortium

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Software

3D-Move

Free Softwares

3D-Move (NEW: Version 1.2) Now Available Online!

Announcement to 3D-Move Users (Posted on August 29, 2010):
Inconsistency Between Text and Excel Output Files of Ver. 1.1



Announcements

DISCUSSION GROUP* at
3d-move.finddiscussion.com to
provide your feedback or
post your questions on the
3D-Move Analysis Software.

The last beta-version of the 3D-Move Analysis (ver 1.1) was released on July, 2010. In 3D-Move, output is provided in formats: Text and Excel. An inconsistency has inadvertently occurred when these two formats were integrated. The **inconsistency was present only in the Excel file**, while the **Text file output is correct**. The origin of the slip-up was traced to the allocation of the columns when the data sharing between Text and Excel output files occurred. Further, there were concerns about the units of the 3D-Move responses being not prominently displayed. These issues have been corrected and a modified beta-version of 3D-Move (ver 1.2) is now available for [download](#)



Freeware Download at:
<http://www.arc.unr.edu/Software.html>



Pavement Analysis

3D-Move Analysis Software - Validation

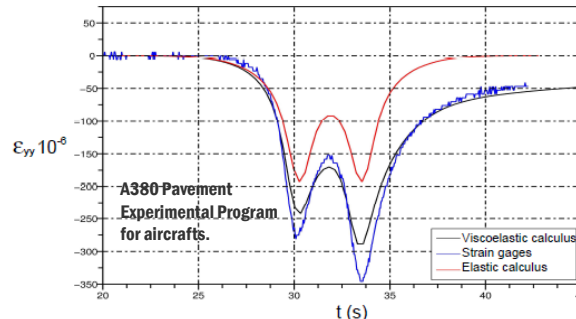


1. 3D-Move vs. ViscoRoute (2010)

- ViscoRoute (IFFSTAR - LCPC): moving circular loaded areas with uniform contact pressure, viscoelastic material properties

Reference:
Chabot, A., Chupin, O., Deloffre, L., and Duhamel, D., "Viscoroute 2.0: a tool for the simulation of moving load effects on asphalt pavement," Road Materials and Pavement Design an International Journal, Volume 11/2, 2010, pp. 227-250.

Loft A., "Evaluation de Viscoroute-v1 pour l'étude de quelques chaussées souples", Msc. Dissertation, Dresden University of Technology speciality Urban and Road construction, 2005.

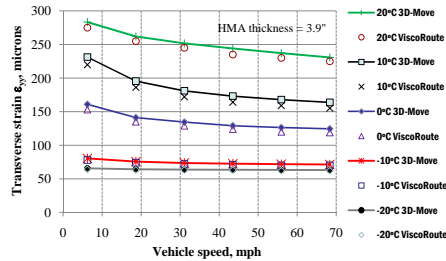


Comparison between elastic computations, ViscoRoute1.0 simulations and transversal strain measurements at the bottom of bituminous layers for a 4-wheels moving load

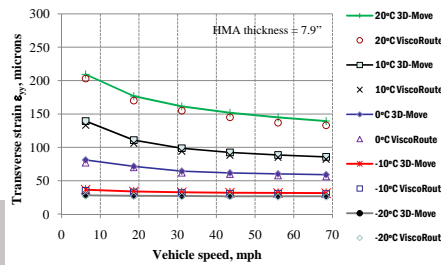


Pavement Analysis

3D-Move Analysis Software - Validation



3D-Move vs. ViscoRoute
 Vehicle speed = 6 to 70 mph
 Pavement temperature = -20°C to 20°C



ViscoRoute Test Results Refer to:
 Chabot, A., Chupin, D., Deloffre, L., and Duhamel, D., "Viscoroute 2.0: a tool for the simulation of moving load effects on asphalt pavement," Road Materials and Pavement Design an International Journal, Volume 11/2, 2010, pp. 227-250.

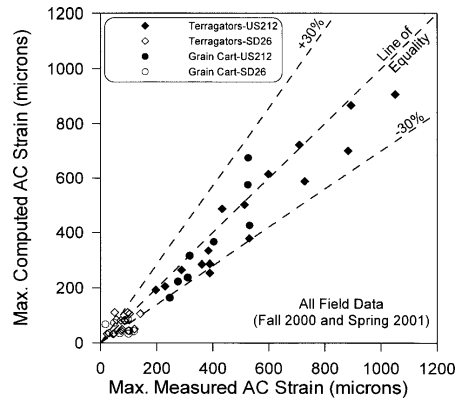
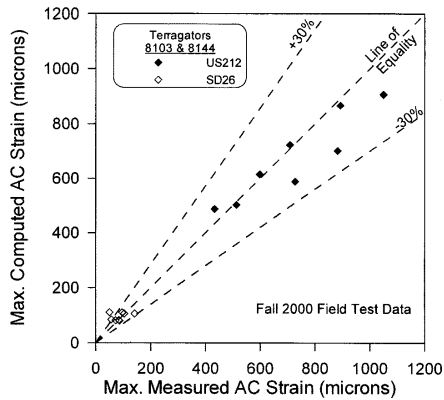


Pavement Analysis

3D-Move Analysis Software - Validation



2. SD Heavy Off-Road Vehicle Field Sections (2000)

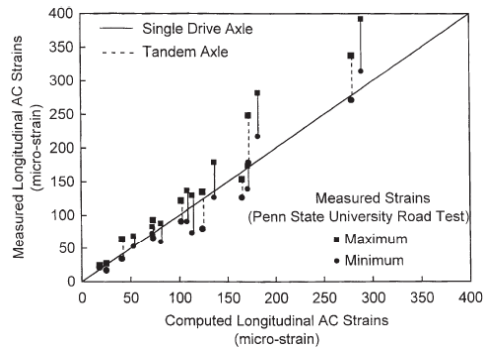
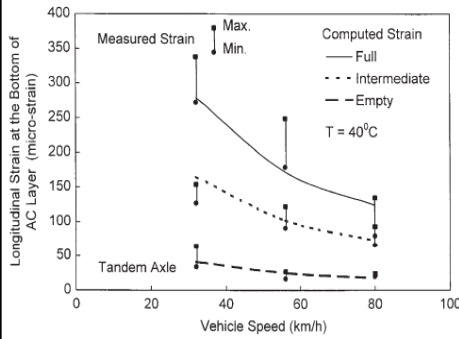


Pavement Analysis

3D-Move Analysis Software - Validation



3. PennState University Test Track (1999)

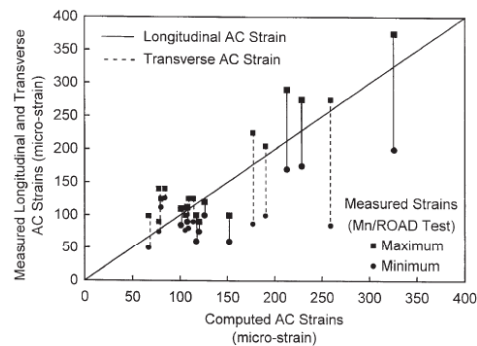
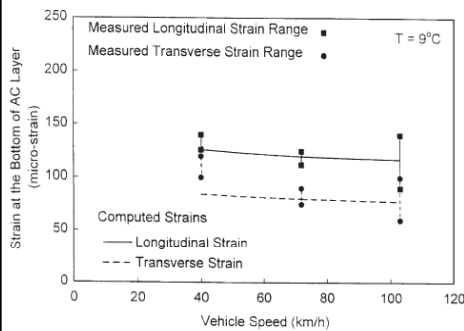


Pavement Analysis

3D-Move Analysis Software - Validation



4. MnRoad (1997)



Database of pavement responses

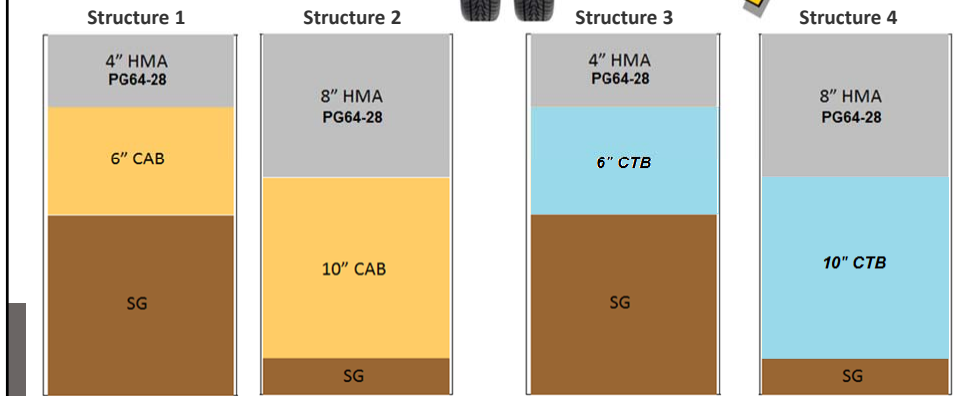


- 10 mph without braking
 - 40 mph without braking
 - 60 mph without braking



HMA layer temp:
 70°F and 104°F

Structures 1 & 2
 pavement analyses
 completed



Pavement Responses Locations



4 inch HMA layer

0.25"	X	X	X	X	X	0.5"
0.5"	X	X	X	X	X	
0.75"	X	X	X	X	X	
1.5"	X	X	X	X	X	1.0"
2.5"	X	X	X	X	X	1.0"
3.5"	X	X	X	X	X	1.0"
4.0"	X	X	X	X	X	

8 inch HMA layer

0.25"	X	X	X	X	X	0.5"
0.5"	X	X	X	X	X	
0.75"	X	X	X	X	X	
1.5"	X	X	X	X	X	1.0"
2.5"	X	X	X	X	X	1.0"
3.5"	X	X	X	X	X	1.0"
6.0"	X	X	X	X	X	4.0"
8.0"	X	X	X	X	X	



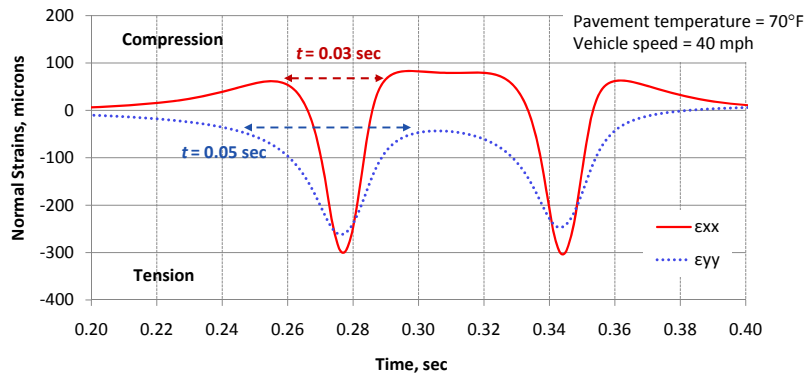
Data analysis completed for responses at center line of the load



Proposed approach to determine f_p



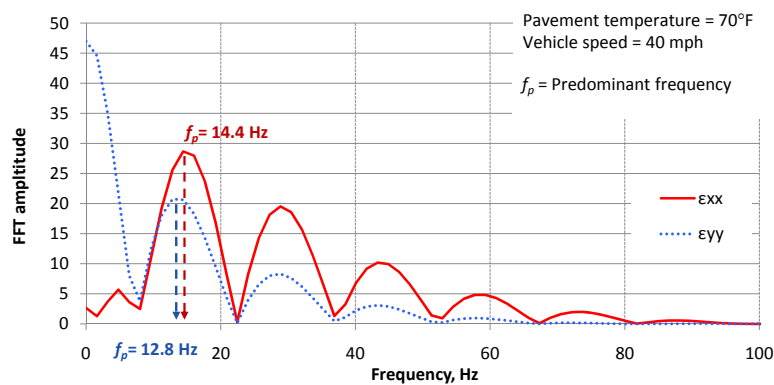
- Example: Bottom of the 4-inch HMA layer:



Proposed approach to determine f_p



- FFT amplitudes of the normal strains of the 4-inch HMA



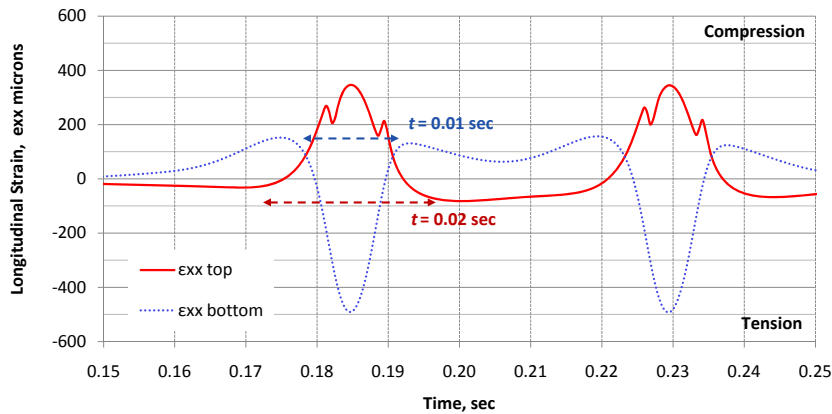
f_p for the 4-inch HMA layer



Case Study	Depth (in)	Predominant frequency, (Hz)							
		σ_{xx}		σ_{yy}		σ_{zz}		σ_{xz}	
		f_p	f_{pred}	f_p	f_{pred}	f_p	f_{pred}	f_p	f_{pred}
Case 1: 70°F and 40 mph	0.25	14.4		12.8		14.4		14.4	
	0.5	14.4		12.8		14.4		14.4	
	0.75	14.4		12.8		14.4		14.4	
	1.5	14.4	14.4	12.8	14.4	14.4	14.4	14.4	14.4
	2.5	14.4		12.8		14.4		14.4	
	3.5	14.4		12.8		14.4		14.4	
Case 2: 104°F and 40 mph	0.25	14.4		12.8		14.4		14.4	
	0.5	14.4		12.8		30.4	30.4	14.4	
	0.75	14.4	14.4	14.4	14.4	30.4	30.4	14.4	14.4
	1.5	12.8		14.4	14.4	30.4	30.4	14.4	14.4
	2.5	30.4		14.4		14.4		14.4	
	3.5	30.4	30.4	14.4	14.4	14.4	14.4	14.4	14.4
Case 3: 70°F and 60 mph	0.25	21.6		19.4		21.6		21.6	
	0.5	21.6		19.4		21.6		21.6	
	0.75	21.6		19.4		19.4		21.6	
	1.5	21.6	21.6	16.8	21.6	21.6	21.6	21.6	21.6
	2.5	21.6		19.4		21.6		21.6	
	3.5	21.6		19.4		21.6		21.6	
Case 4: 104°F and 60 mph	0.25	21.6		19.4		43.3		21.6	
	0.5	21.6		19.2		43.3		21.6	
	0.75	21.6	21.6	19.2	21.6	43.3	43.3	21.6	21.6
	1.5	21.6		21.6	21.6	43.3		21.6	21.6
	2.5	43.3		21.6		21.6		21.6	
	3.5	43.3	43.3	21.6	21.6	21.6	21.6	21.6	21.6
Case 5: 70°F and 10 mph	0.25	3.6		3.2		3.6		3.6	
	0.5	3.6		3.2		3.6		3.6	
	0.75	3.6		3.2		7.6	7.6	3.6	3.6
	1.5	3.2	7.6	3.2	3.6	7.6	7.6	3.6	3.6
	2.5	7.6		3.6		3.6		3.6	
	3.5	4		3.6		3.6	3.6	3.6	3.6
Case 6: 104°F and 10 mph	0.25	7.6		3.2		7.6		3.6	
	0.5	7.6		3.2		7.6	7.6	3.6	3.6
	0.75	7.6	7.6	3.2	3.6	7.6	7.6	3.6	3.6
	1.5	11.2		3.6	3.6	3.6		3.6	3.6
	2.5	11.2		3.6		3.6		3.6	
	3.5	11.2	11.2	3.6	3.6	3.6	3.6	3.6	3.6

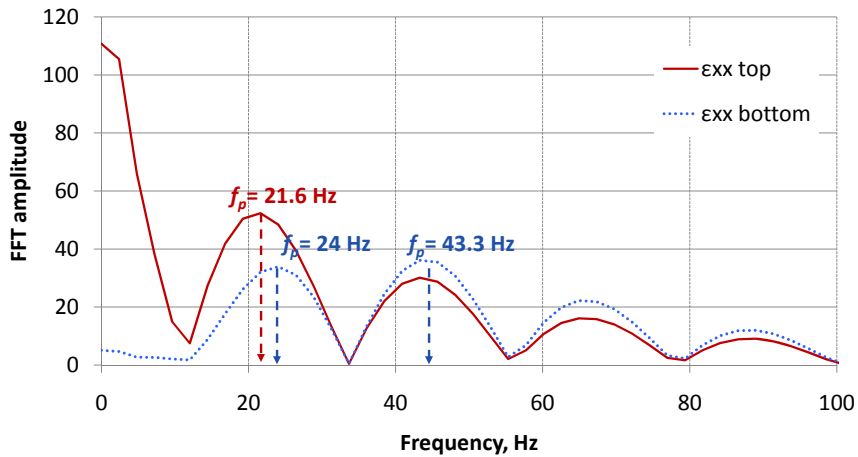


Case 4 Predominant Frequencies Temp = 104°F, V = 60 mph, Tensile Strain ϵ_{xx}



Case 4 Predominant Frequencies

Temp = 104°F, V = 60 mph, Tensile Strain ϵ_{xx}



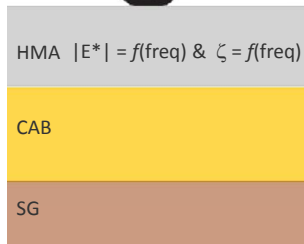
Pseudo-Dynamic Analysis



Viscoelastic



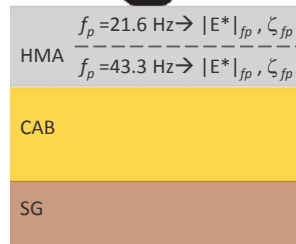
Velocity = 60 mph



Pseudo-dynamic



Velocity = 60 mph

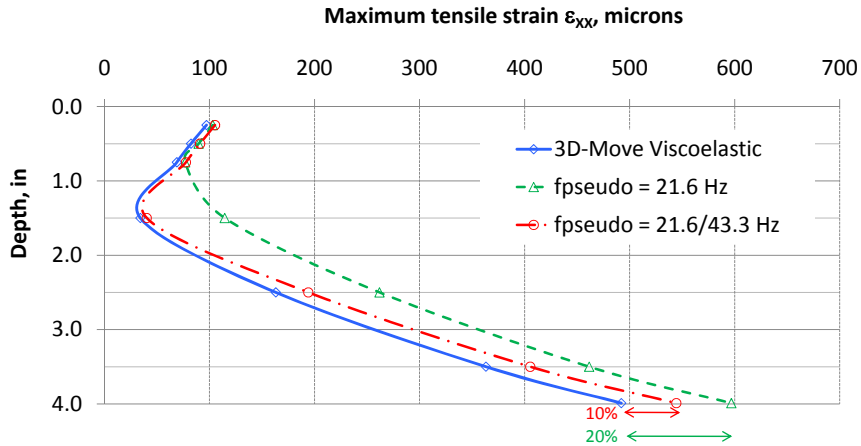


Pavement responses

Pavement responses

Case 4 Pseudo-Dynamic Analysis

Temp = 104°F, V = 60 mph, Tensile Strain ϵ_{xx}



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f_p for the 8-inch HMA layer



Case Study	Depth* (in)	Predominant frequency, (Hz)									
		ϵ_{xx}		σ_{xy}		ϵ_{zz}		σ_{zz}			
		f_p	f_{pseudo}	f_p	f_{pseudo}	f_p	f_{pseudo}	f_p	f_{pseudo}	f_p	f_{pseudo}
Case 7: 70°F and 40 mph	0.25	12.8		16		30.4		14.4			
	0.5	12.8		11.2		30.4		14.4			
	0.75	12.8	12.8	9.6		30.4	30.4	14.4			
	1.5	12.8		14.4		30.4		14.4			
	2.5	12.8		14.4		30.4		14.4			
	3.5	30.4		14.4		14.4		14.4			14.4
	6	30.4	30.4	12.8		12.8	12.8	14.4			14.4
Case 8: 104°F and 40 mph	0.25	14.4		12.8		30.4		14.4			
	0.5	14.4		12.8		30.4		14.4			
	0.75	14.4	14.4	11.2		30.4	30.4	14.4			
	1.5	12.8		12.8		30.4		14.4			
	2.5	30.4		12.8		14.4		14.4			14.4
	3.5	30.4		12.8		14.4		14.4			14.4
	6	30.4	30.4	12.8		14.4	14.4	14.4			14.4
Case 9: 70°F and 60 mph	0.25	19.2		19.2		19.2		21.6			
	0.5	19.2		16.8		40.8		21.6			
	0.75	19.2	19.2	16.8		45.7	45.7	21.6			
	1.5	19.2		19.2		45.7		21.6			21.6
	2.5	19.2		19.2		45.7		21.6			21.6
	3.5	45.7		21.6		21.6		21.6			21.6
	6	45.7	45.7	19.2		19.2	19.2	21.6			21.6
Case 10: 104°F and 60 mph	0.25	21.6		19.2		45.7		21.6			
	0.5	21.6		16.8		45.7	45.7	21.6			
	0.75	19.2	21.6	16.8		21.6	21.6	21.6			
	1.5	45.7		21.6		21.6		21.6			21.6
	2.5	45.7		21.6		21.6		21.6			21.6
	3.5	43.3		21.6		21.6	21.6	21.6			21.6
	6	43.3	45.7	21.6		21.6	21.6	21.6			21.6
Case 11: 70°F and 10 mph	0.25	3.6		3.2		7.6		3.6			
	0.5	3.6		3.2		7.6		3.6			
	0.75	3.6	3.6	3.2		7.6	7.6	3.6			
	1.5	3.6		3.6		7.6		3.6			3.6
	2.5	3.6		3.6		7.6		3.6			3.6
	3.5	7.6		3.6		7.6		3.6			3.6
	6	3.6	7.6	3.2		3.6	3.6	3.6			3.6
Case 12: 104°F and 10 mph	0.25	3.6		3.2		7.6		3.6			
	0.5	3.6		3.2		7.6		3.6			
	0.75	3.2	3.6	3.6		7.6	7.6	3.6			
	1.5	11.2		3.6		3.6		3.6			3.6
	2.5	11.2		3.6		3.6		3.6			3.6
	3.5	11.2	11.2	3.6		3.6	3.6	3.6			3.6
	6	3.6	3.6	3.2		3.6	3.6	3.6			3.6

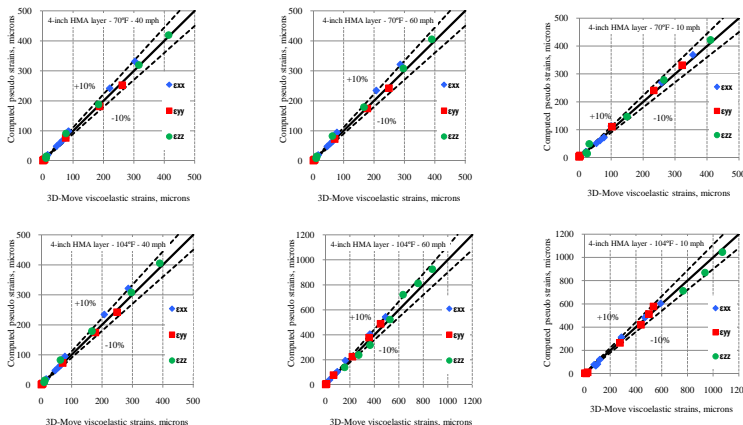
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Viscoelastic vs. Pseudo-Dynamic analysis



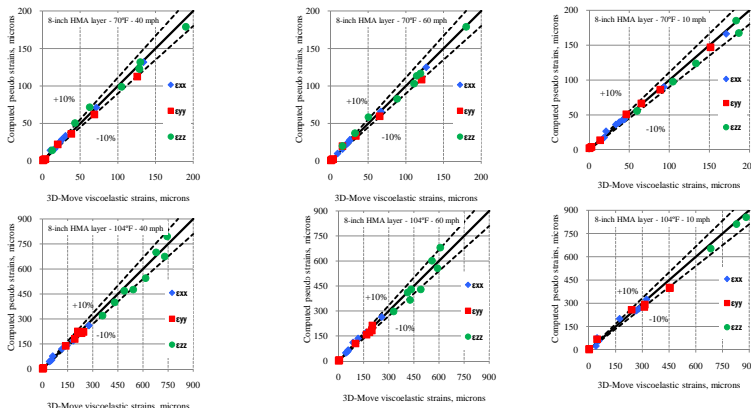
4-inch HMA layer



Viscoelastic vs. Pseudo-Dynamic analysis



8-inch HMA layer



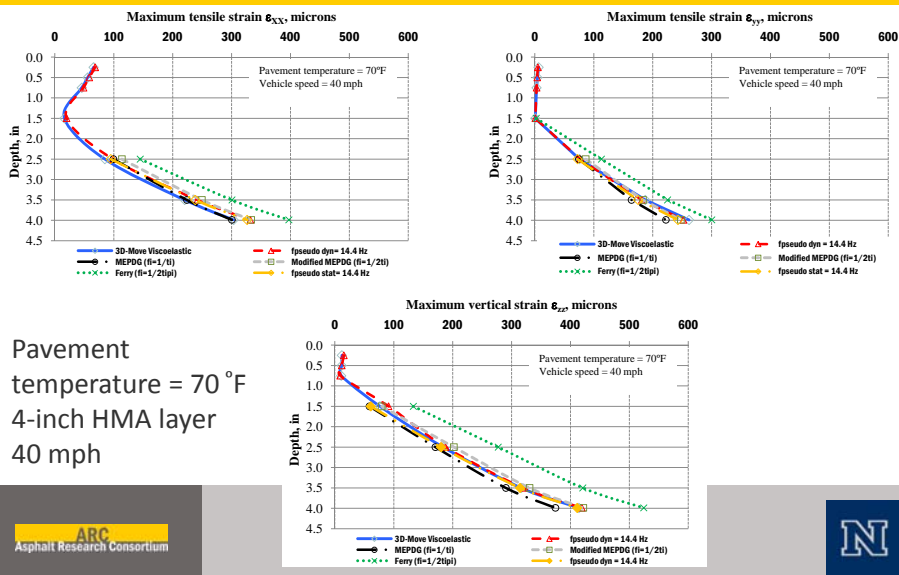
Pseudo-Static Analysis



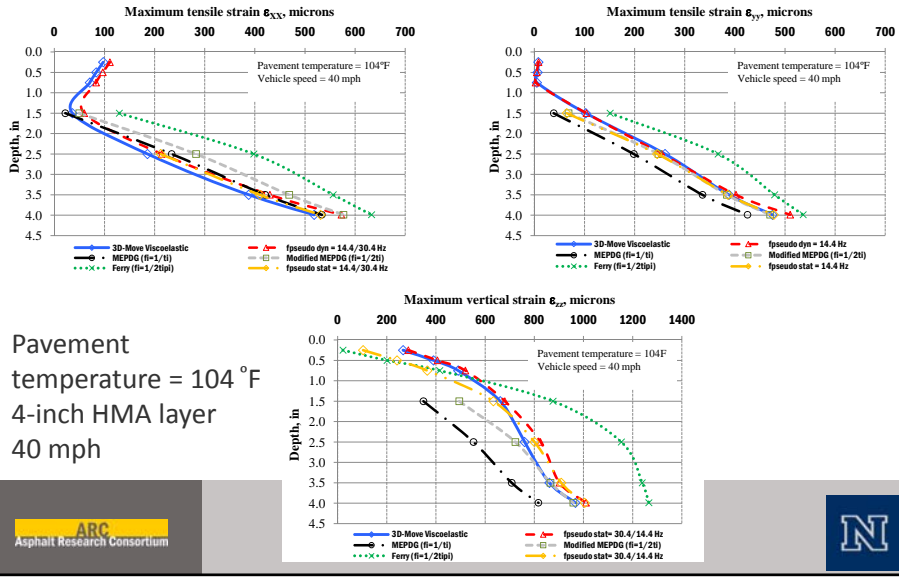
- **Pseudo-Static:**
 - Vehicle speed = 0
 - Linear Elastic Analysis (LEA)
 - Use f_p to select $|E^*|_{f_p}$
 - Damping $\zeta_{f_p} = 0$
- Also Compare pavement responses following
 - MEPDG approach ($f = 1/t$)
 - Modified MEPDG ($f = 1/(2t)$)
 - Ferry ($f = 1/(2\pi t)$)



Pavement responses comparison



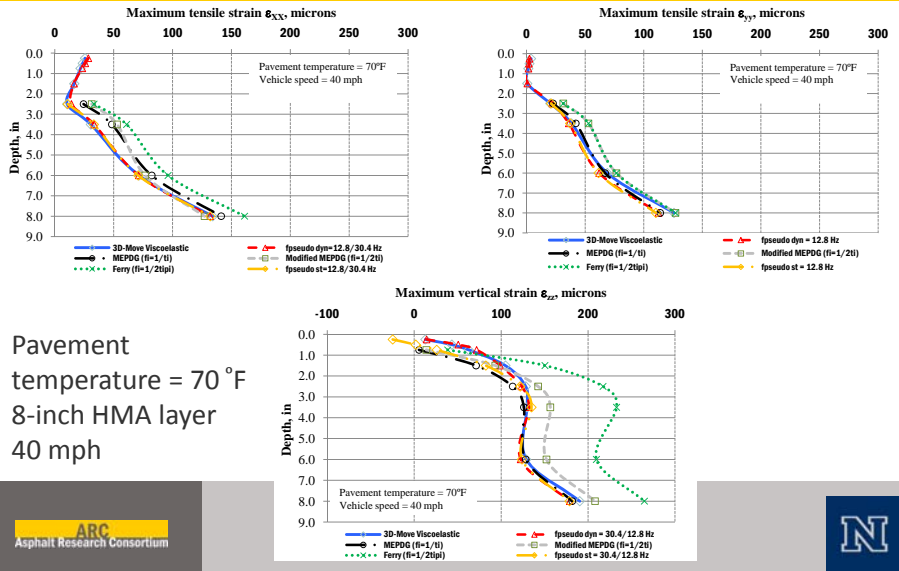
Pavement responses comparison



Pavement temperature = 104 °F
4-inch HMA layer
40 mph



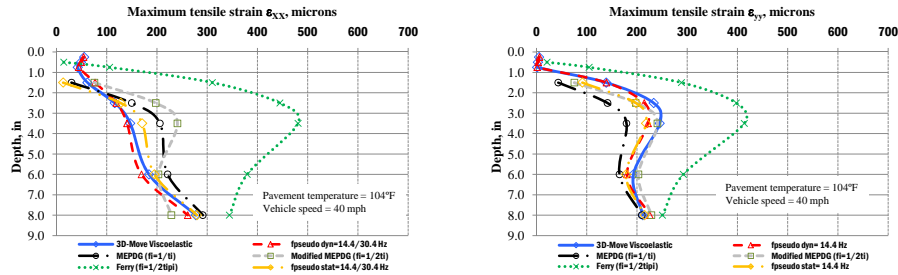
Pavement responses comparison



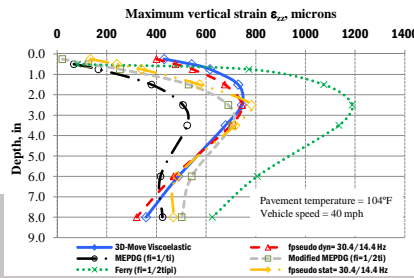
Pavement temperature = 70 °F
8-inch HMA layer
40 mph



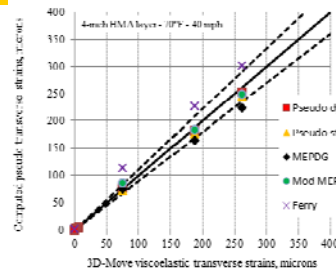
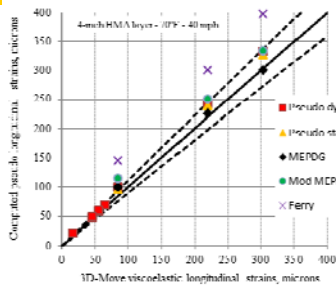
Pavement responses comparison



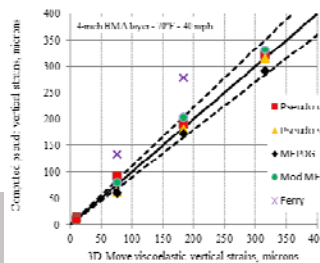
Pavement temperature = 104 °F
8-inch HMA layer
40 mph



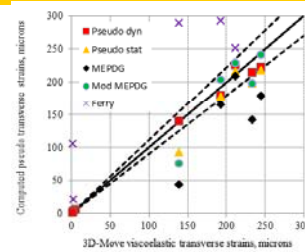
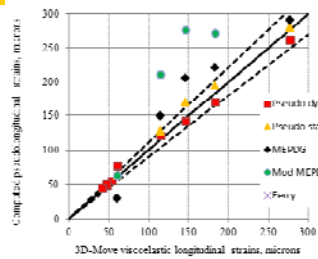
Pavement responses comparison



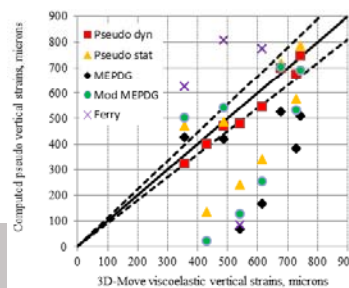
Pavement temperature = 70 °F
4-inch HMA layer



Pavement responses comparison



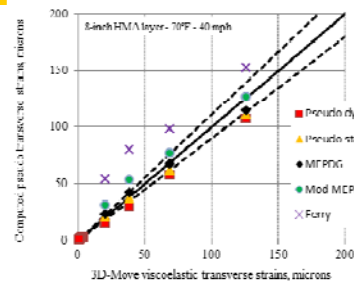
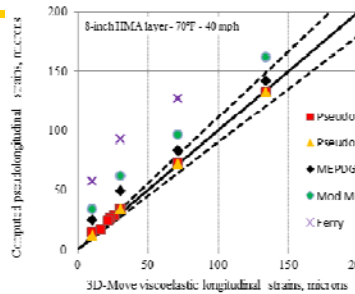
Pavement temperature = 104 °F
4-inch HMA layer



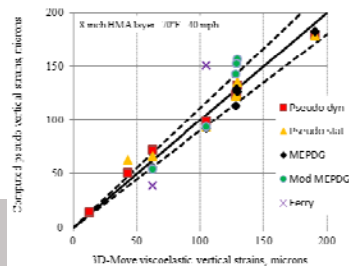
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Pavement responses comparison



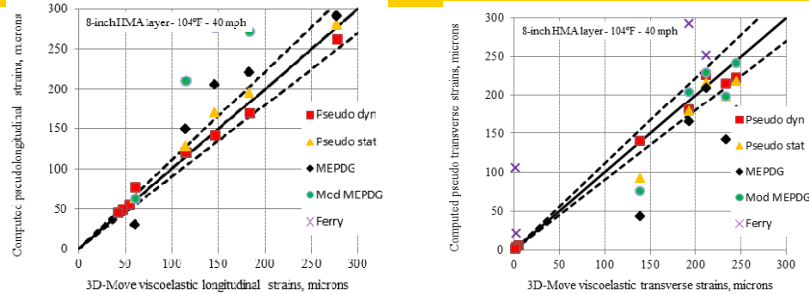
Pavement temperature = 70 °F
8-inch HMA layer



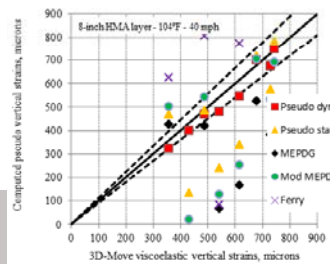
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Pavement responses comparison



Pavement temperature = 104 °F
8-inch HMA layer



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Overall Findings



- Use of one single set of f_p cannot be assigned to the AC layer to study all responses.
- Pavement responses can be successfully predicted (within $\pm 10\%$) by *Pseudo-Dynamic* equivalent approach.
- MEPDG approach derives in comparable pavement responses only when asphalt layer is stiff and there are no multiple f_p within the asphalt layer.

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Additional needed work...



- Investigate influence of axle load, response location and axle configuration on f_p .
 - Investigate influence of CTB on f_p .
 - Evaluate different time-frequency conversions.
 - Other!
- ...Feedback...

Acknowledgment



- This work is part of the overall effort in the Asphalt Research Consortium (ARC) work element E2d. (www.arc.unr.edu)
- FHWA support gratefully acknowledged.
- Contents reflect the views of the authors and do not necessarily reflect the official views & policies of FHWA.